

# On Simulation and Optimization of Freeway Network Operations

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# **Progress from last PSG meeting**

- 1 Optimization of Traffic Flow under non-recurrent events using reinforcement learning-based VSL and RM
2. Control of ramp metering Using Deep Koopman model

# 1. Optimization of Traffic Flow under non-recurrent events using reinforcement learning-based VSL and RM controls

**B. Wiwatanapataphee, Yong Hong Wu**

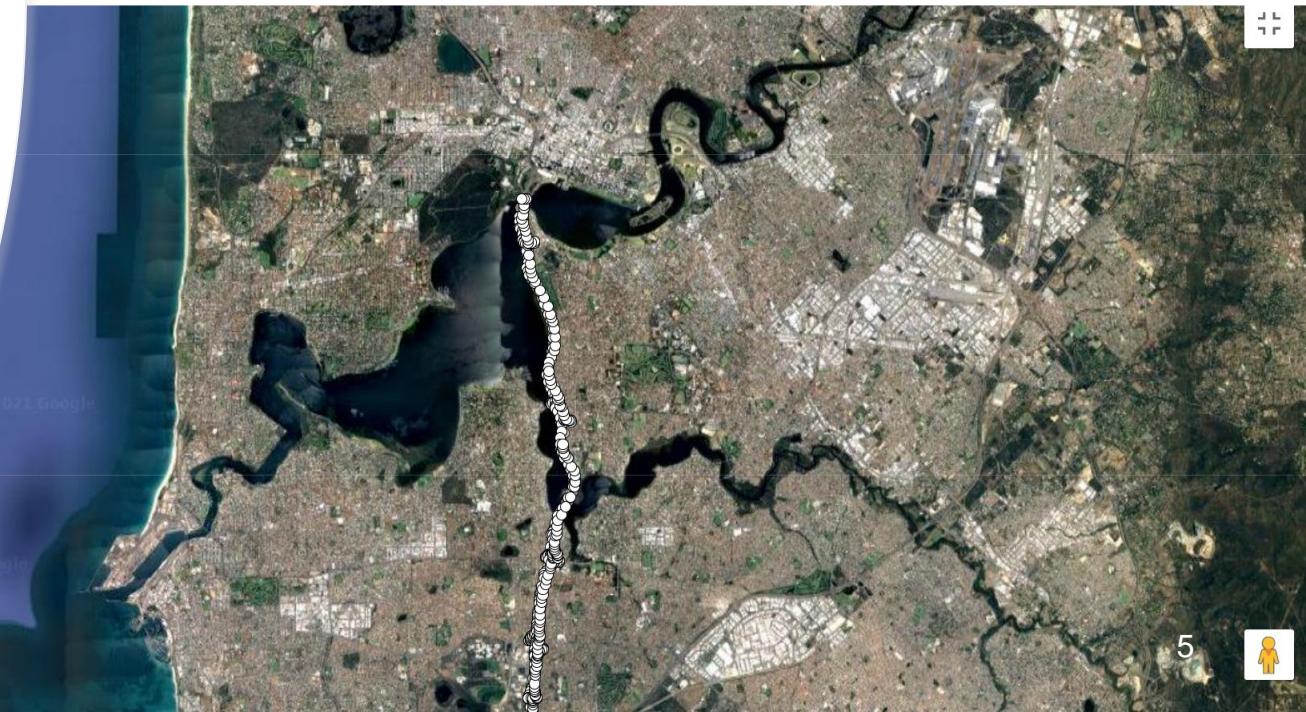
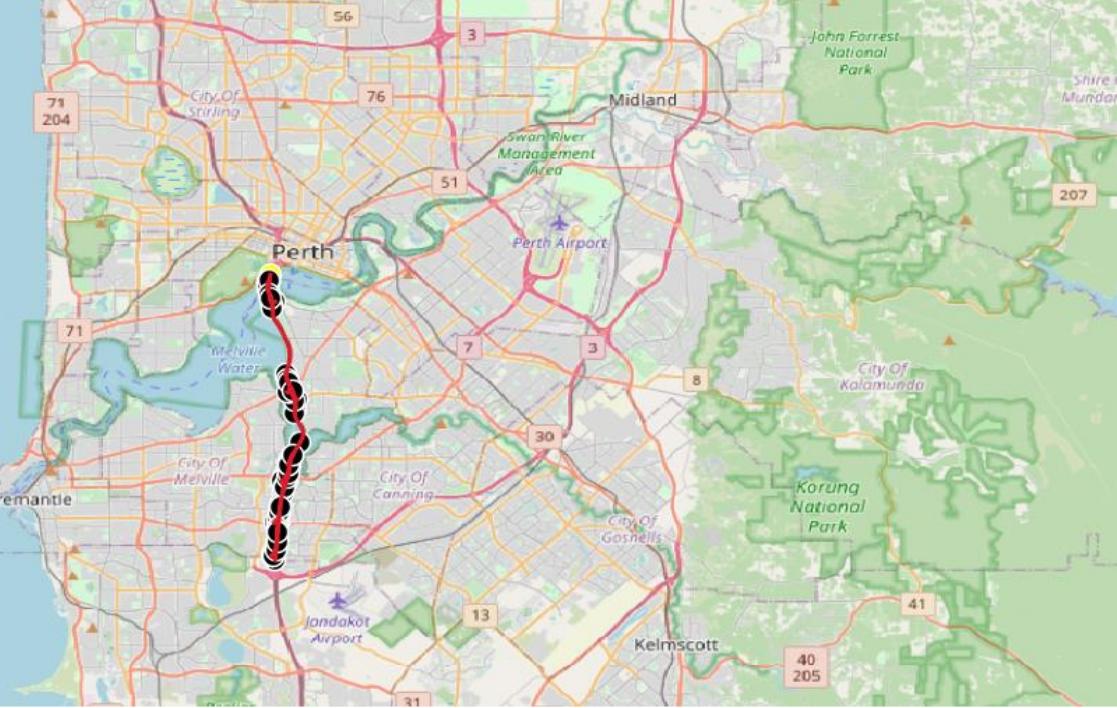


## Outline

- (1) Road Network model
- (2) Optimisation model for RM and VSL parameters
- (3) Computational experiments

# (1) Road Network Model

Kwinana Fwy Network from  
Farrington RD. to Narrows Bridge

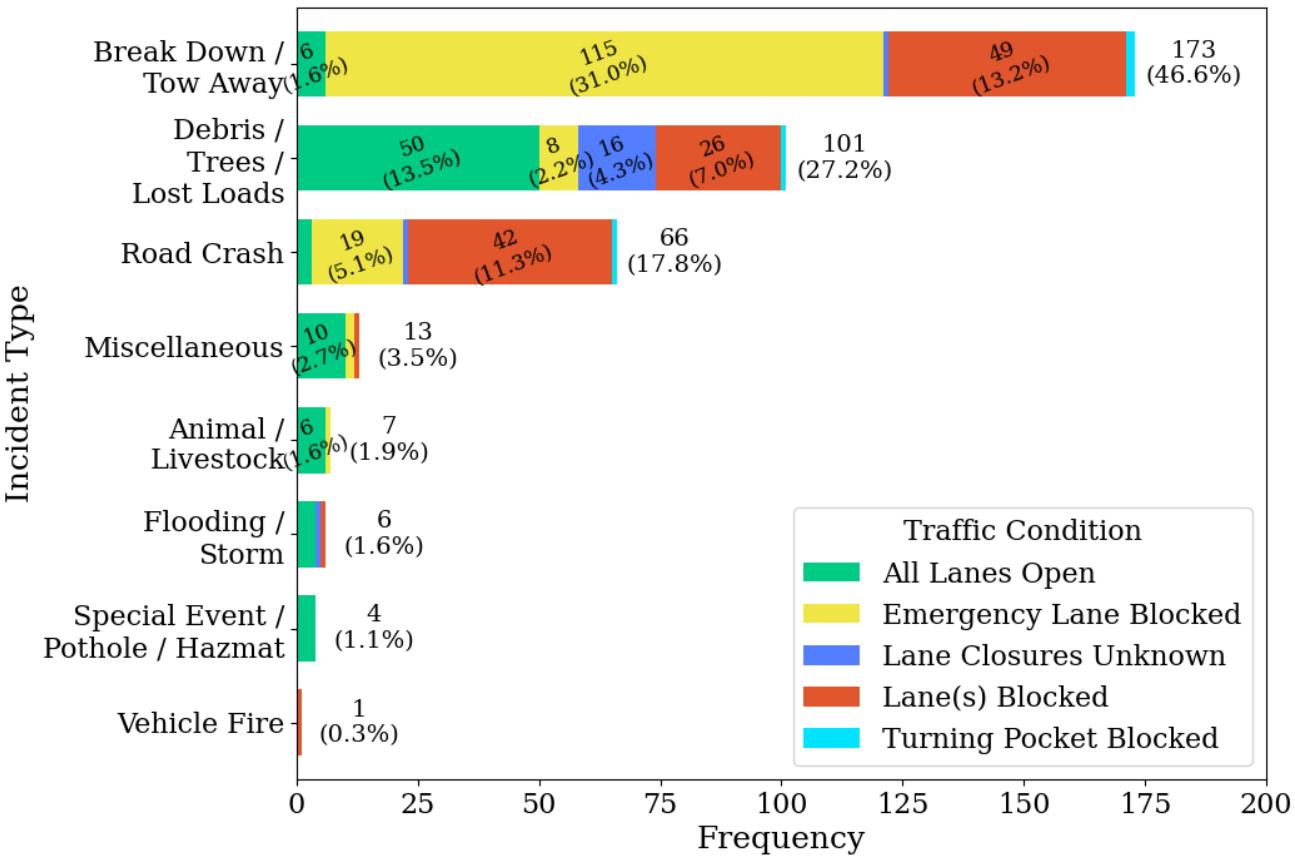
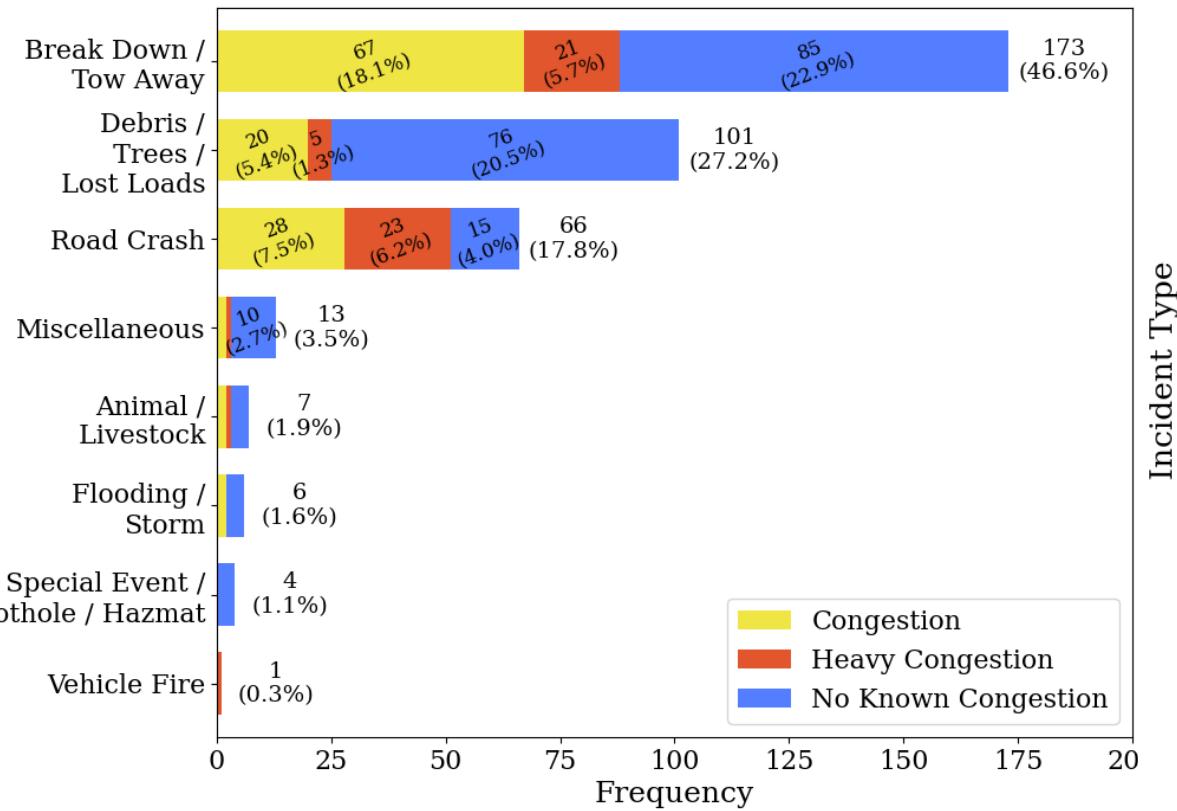


# Network information

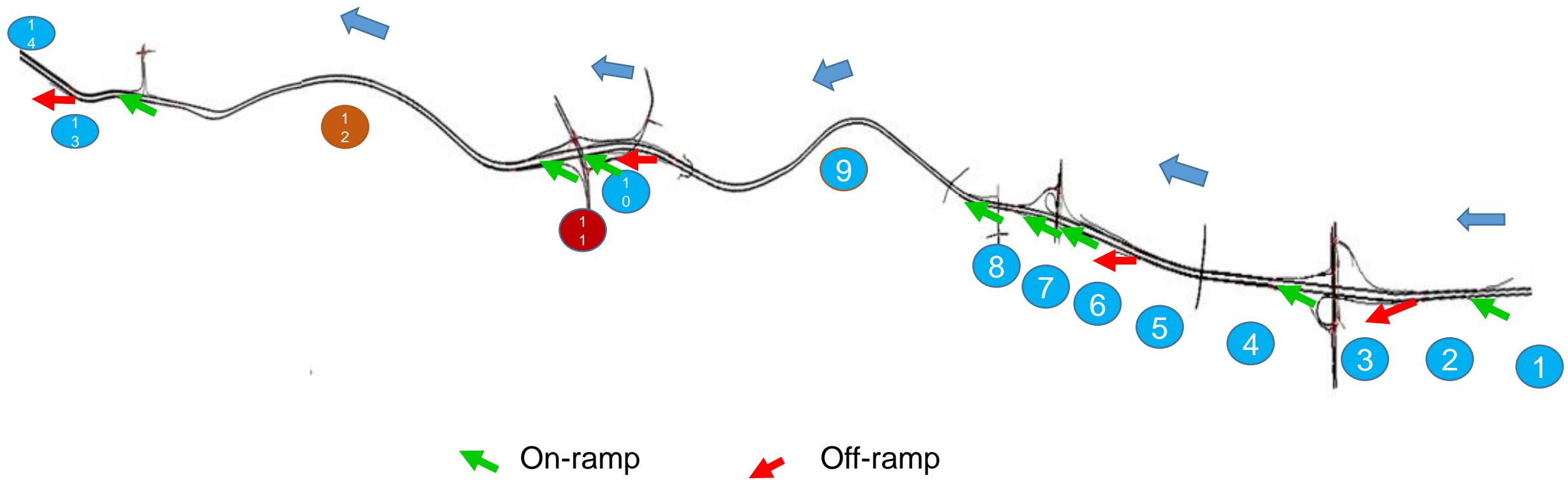
Edge	From	To	Length	Lanes	RM/VSL	VDS	Remarks
1	J1	H622	540.62	3		0091, 0200	
2	H622	J2	150.74	4	RM	0090	Farrington RD.
3	J2	H618	226.09	4		0190	
4	H618	J4	215.70	4			
5	J4	J5	398.23	3			
6	J5	H617	389.89	3		0089	
7	H617	J7	268.88	5	RM	0180, 0700	South St.
8	J7	J8	146.65	4			
9	J8	H559	590.53	4			
10	H559	H558	587.50	3		0170, 0702	Leach Hwy SB
11	H558	J11	230.21	4	RM		
12	J11	H554	211.05	3		0160	
13	H554	J13	123.91	4	RM		Leach Hwy NB
14	J13	H553	189.17	3		0088,0150	
15	H553	J15	227.38	4	RM		Cranford AV.
16	J15	J16	48.68	3			
17	J16	J17	685.48	3			
18	J17	J18	1435.18	3	VSL	0087, 0140, 0086	
19	J18	H551	293.21	3			
20	H551	H547	545.83	3	VSL	0130	
21	H547	J21	127.12	4			Canning SB Man.
22	J21	J22	128.3	3		0085	
23	J22	J23	273.33	3			
24	J23	J24	37.84	4			
25	J24	H549	130.44	3		0084	
26	H549	J26	134.99	4	VSL	0120	Canning NB
27	J26	J27	79.65	4	VSL		
28	J27	J28	3170.18	3	VSL	0003, 0083,0100,0082	
29	J28	J29	148.32	3	VSL		
30	J29	H500	370.6	4	VSL	0081	
31	H500	J31	119.89	4	VSL		Mill Pts
32	J31	H503	259.97	4	VSL		
33	H503	J33	239.04	5		0080	
34	J33	J34	363.95	5			

# Road incidents on the Kwinana Freeway

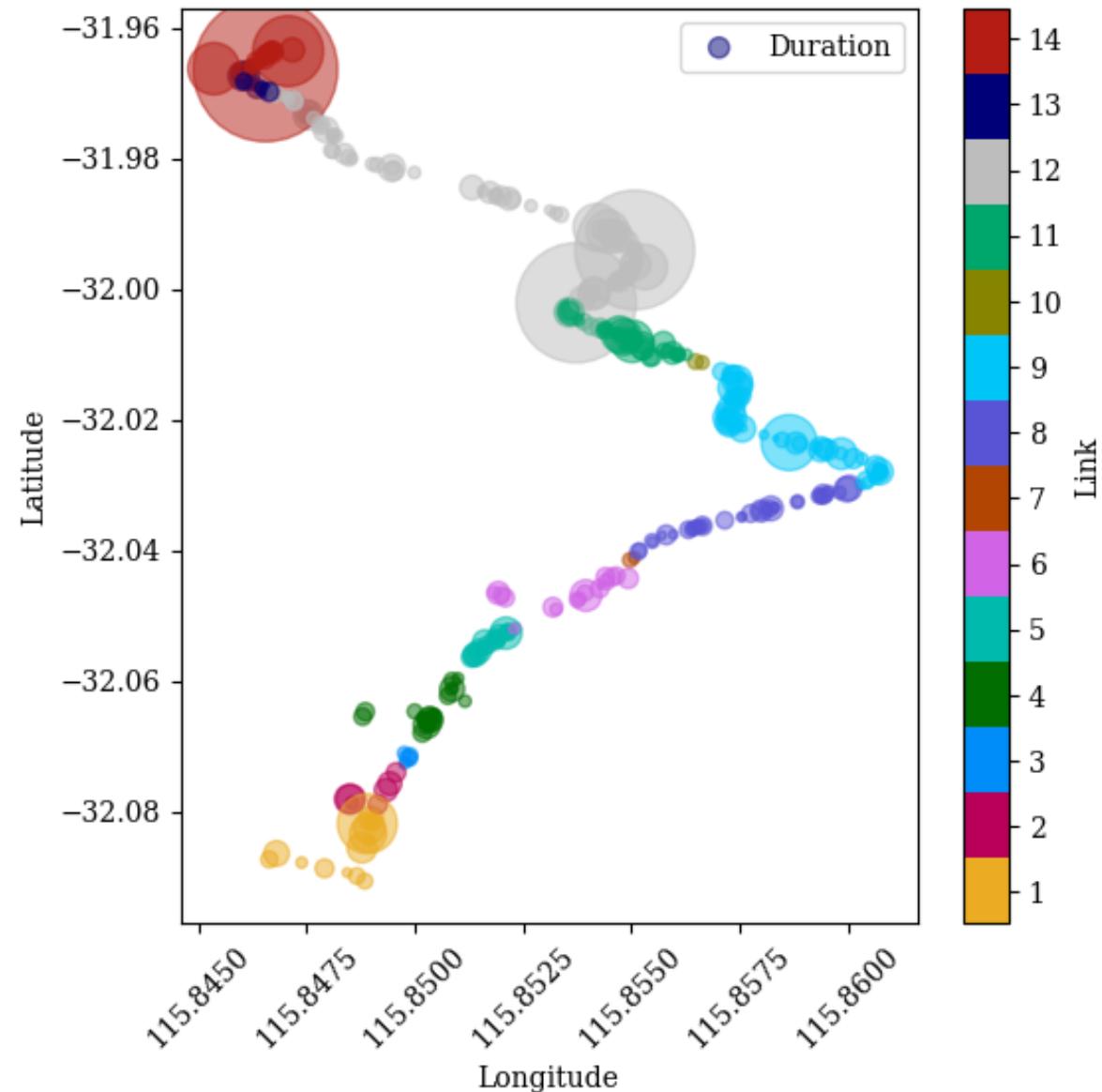
## Northbound 1 January 2018 - 25 October 2018



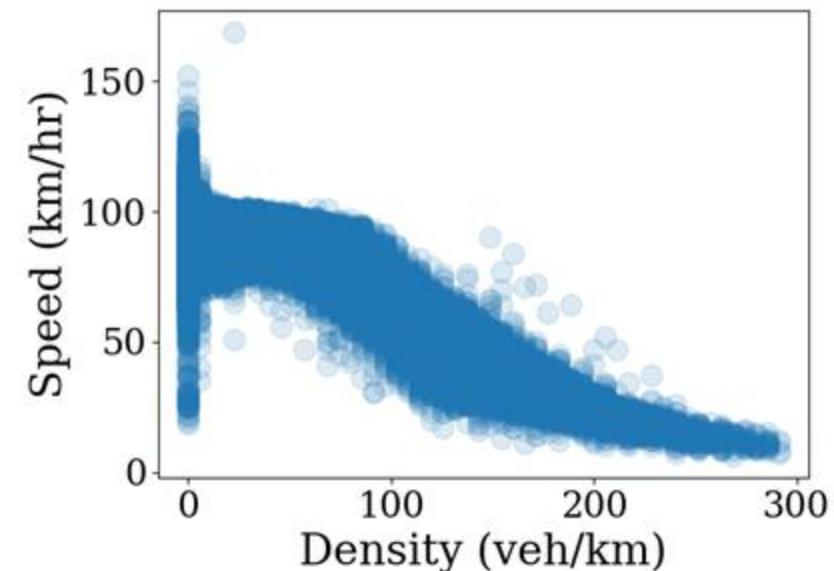
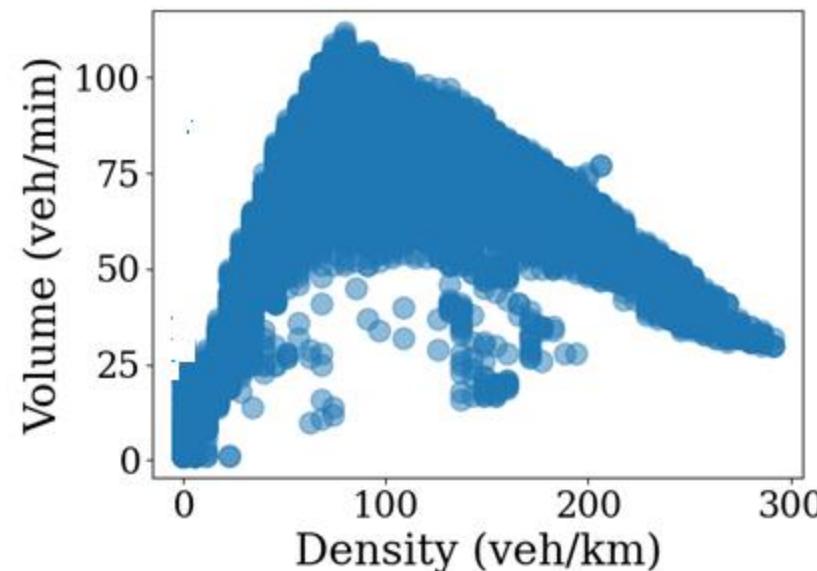
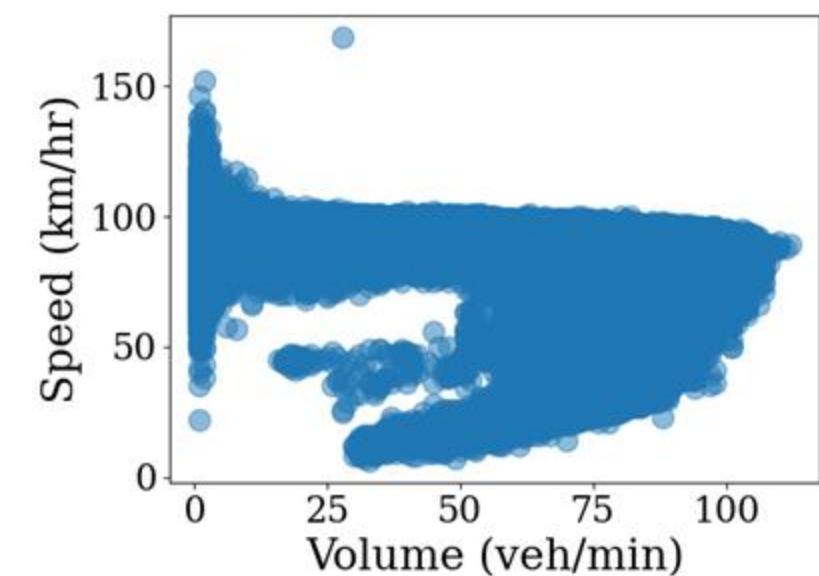
# 14 Links of the Kwinana Freeway Northbound



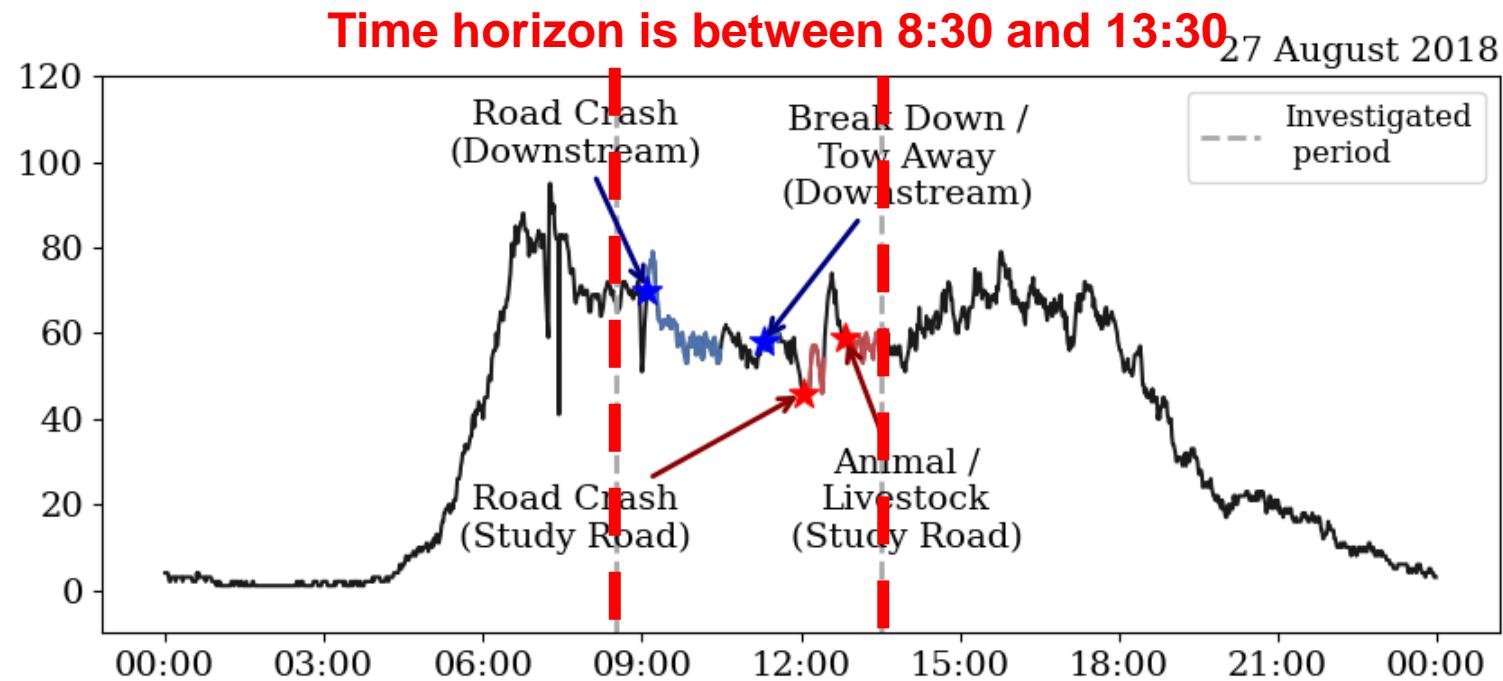
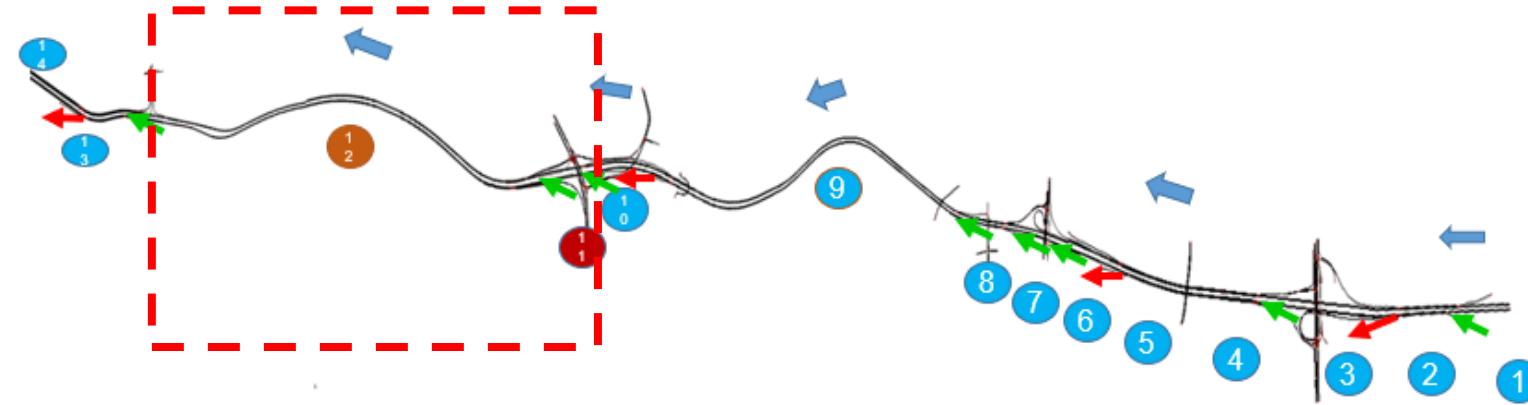
# Duration of road incidents occurring on the Kwinana Freeway northbound from NPI link 1 to 14

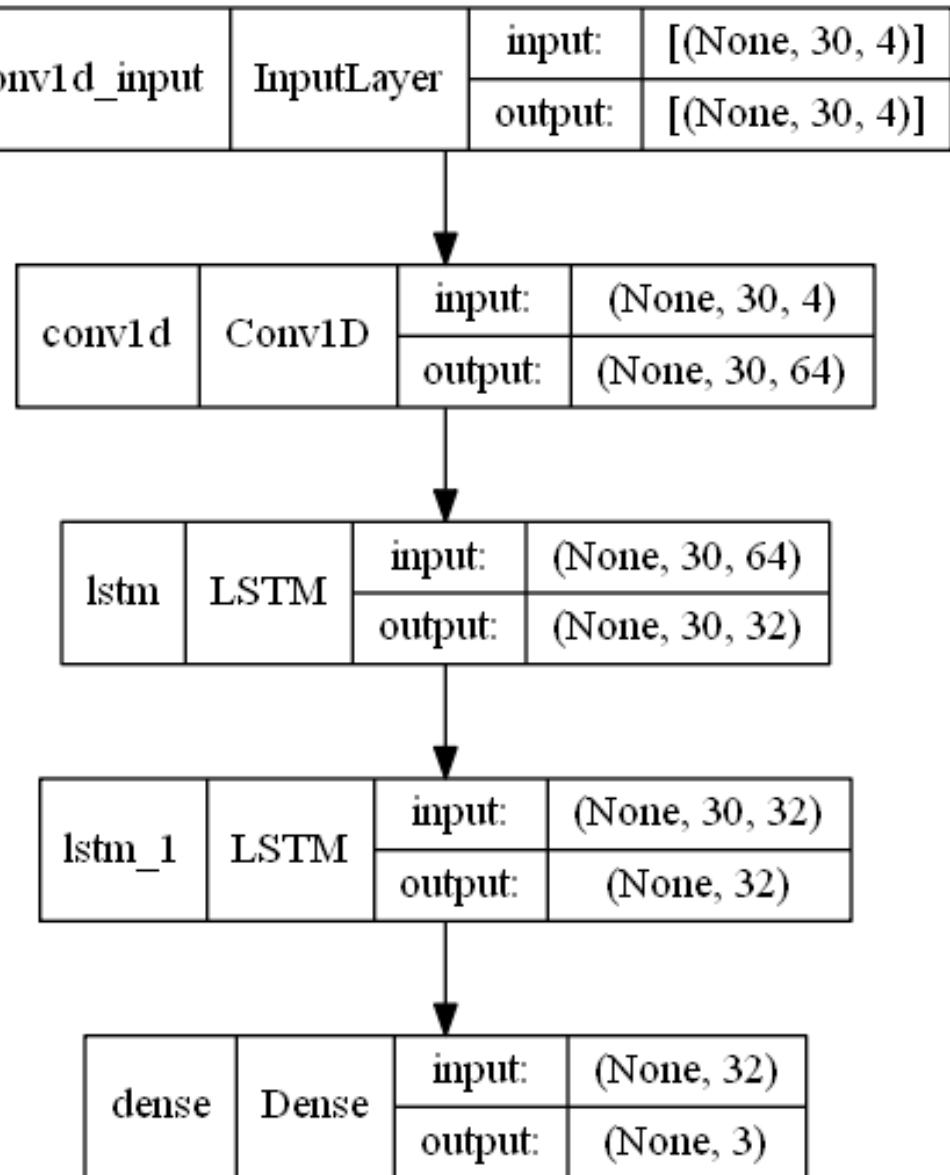


# Fundamental diagrams

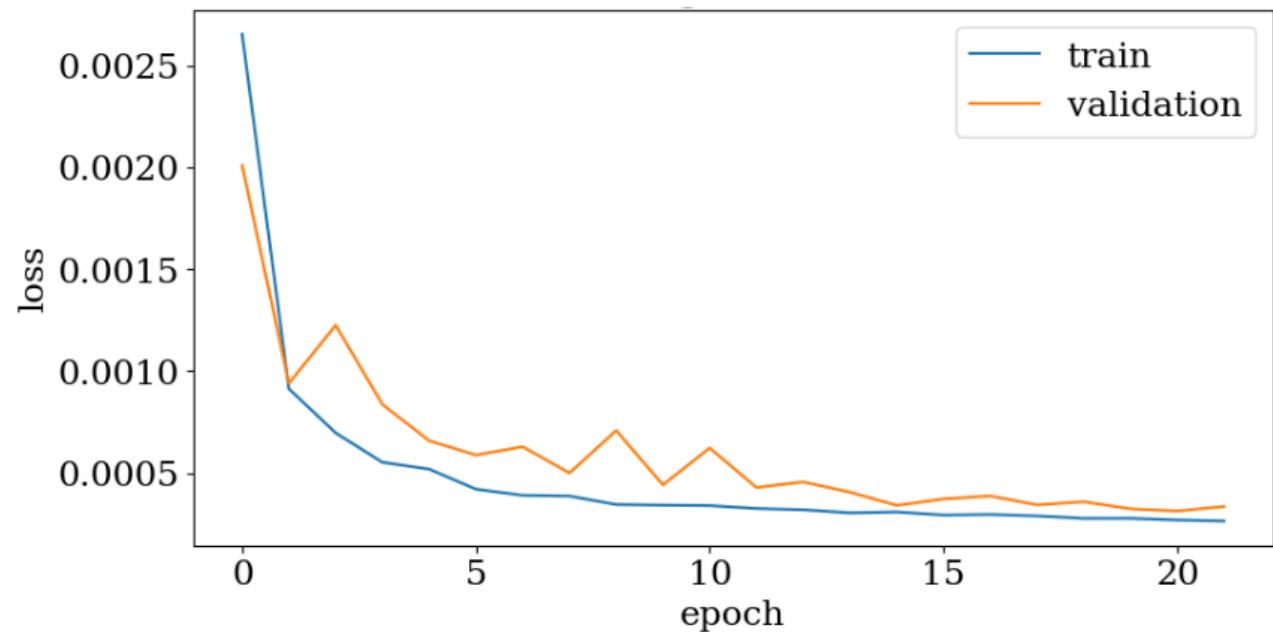


# Observed traffic flow under road incidents

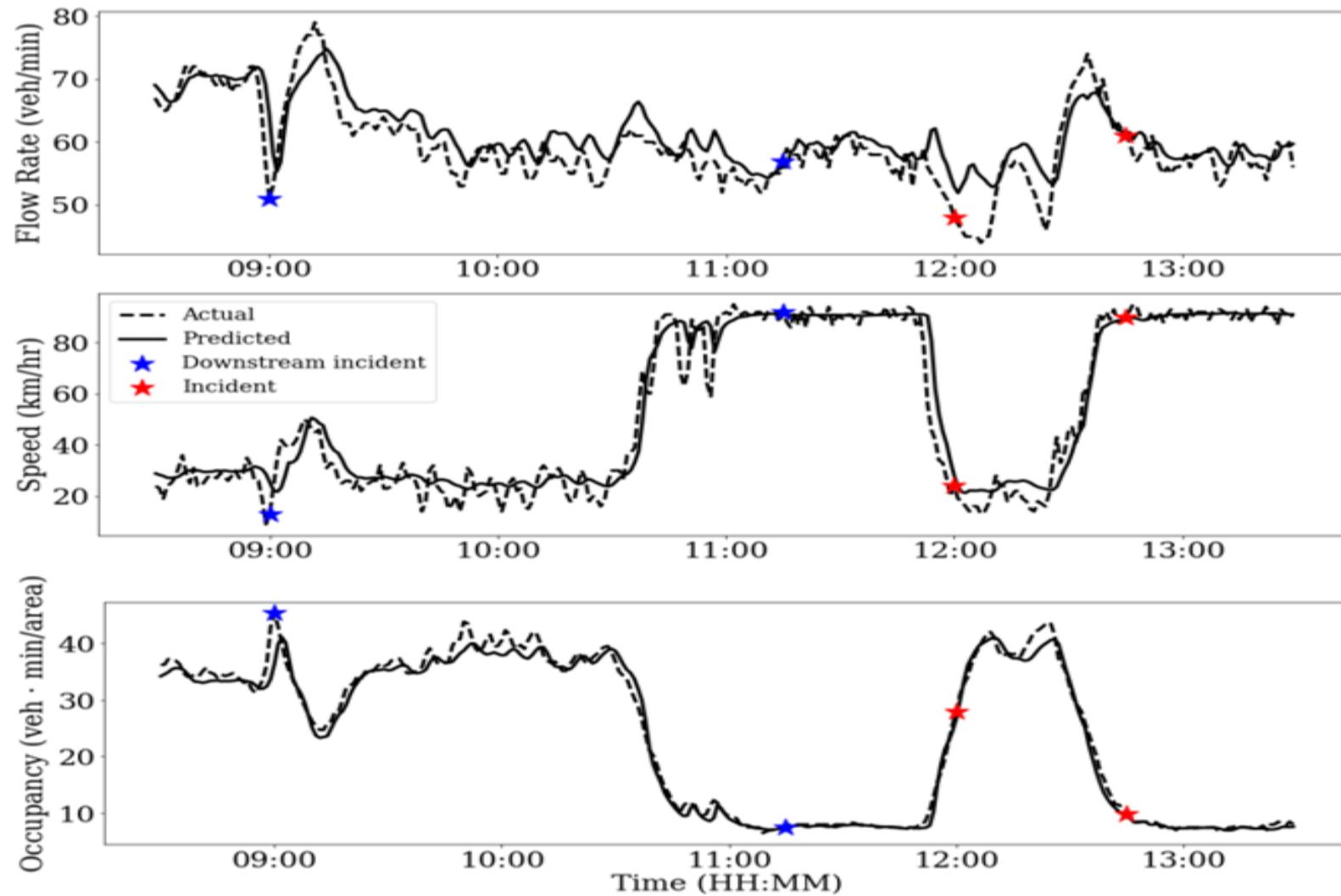




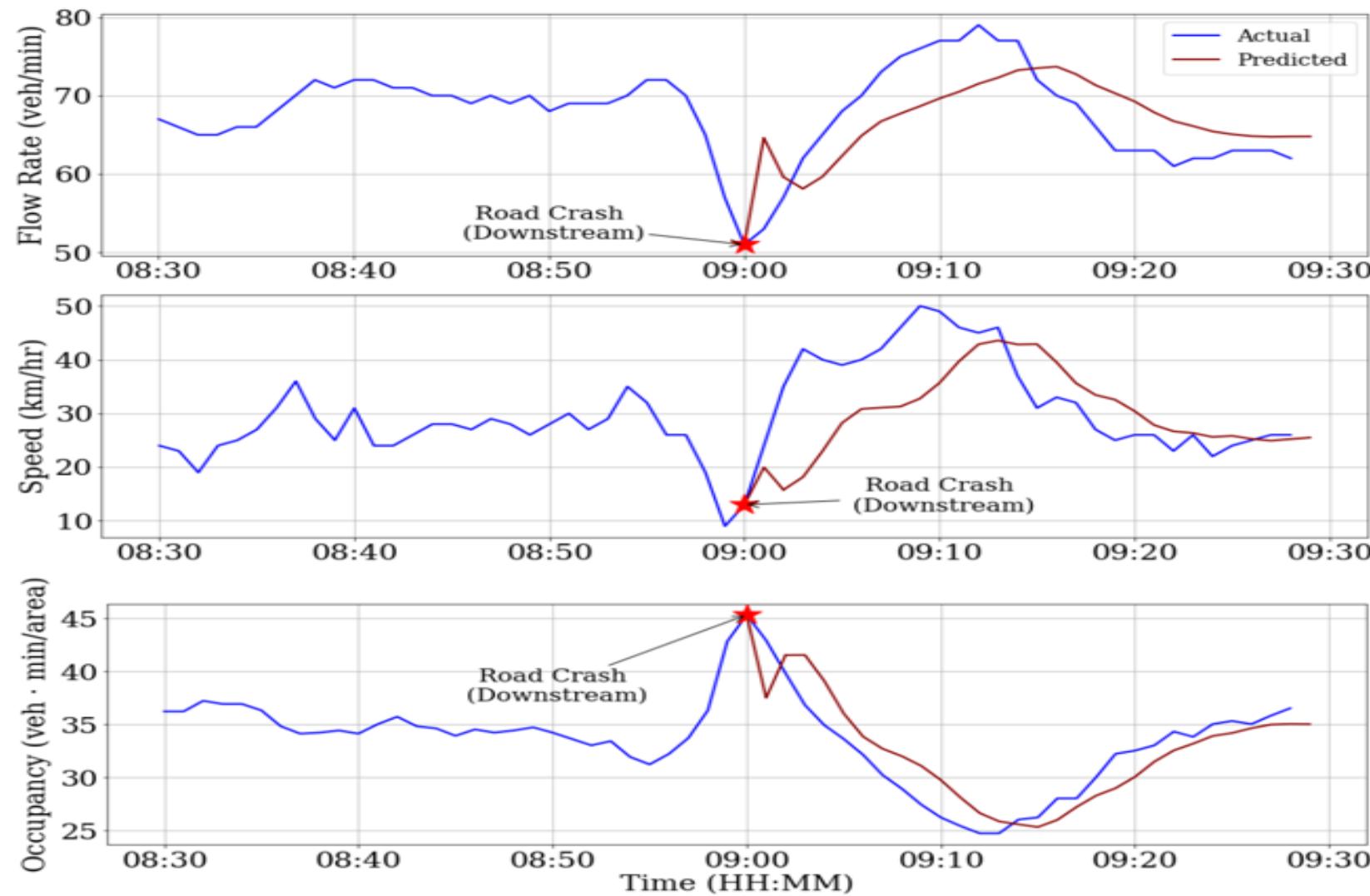
# Traffic prediction under non-recurrent events using 1-D CNN LSTM model



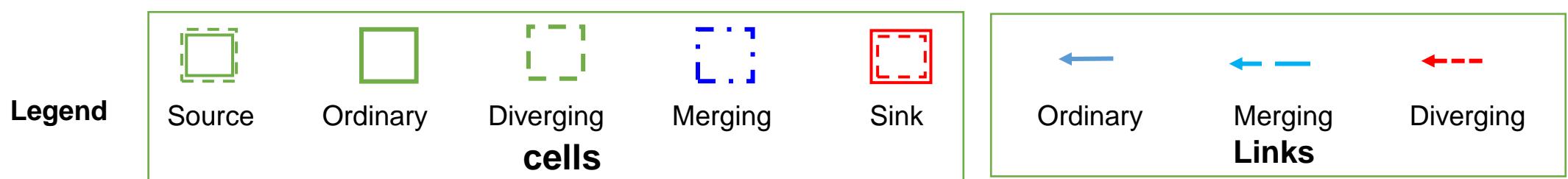
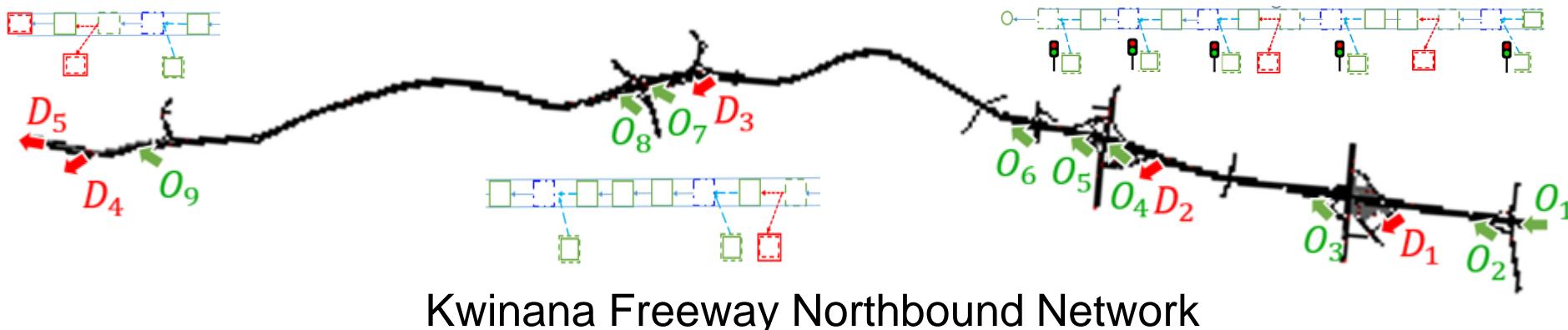
# Long-term predictions



# Short-term predictions



## (2) Optimisation model for RM and VSL parameters



# The optimisation model:

$$\min \sum_{t=\tau}^{t_{end}} T \left( \sum_{i=1}^{rs} L_i k_i(t) \right) + \lambda_{rm} \sum_{t=\tau+1}^{t_{end}-1} \sum_{i=1}^{rs_{rm}} (\alpha_i(t) - \alpha_i(t-1))^2 + \lambda_{vsl} \sum_{t=\tau+1}^{t_{end}-1} \sum_{i=1}^{rs_{vsl}} (\beta_i(t) - \beta_i(t-1))^2$$

- $\frac{n_i \partial k_i}{\partial t} + \frac{\partial}{\partial x} \Delta q_i(t) = 0, \quad 0 \leq k_i(t) \leq k_{jam,i}$

$$\Delta q_i(t) = q_i^{in}(t-1) - q_i^{out}(t-1) + r_i(t-1) - s_i(t-1)$$

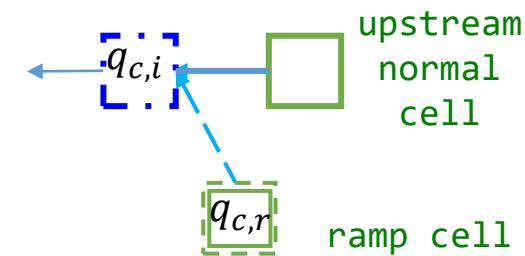
$$r_i(t) = \min \left[ n_{i,r} q_{c,r}; \beta_{i,r} v_{f,r} k_{i,r}(t-1); \max \{ r_i^\alpha(t); queue_{i,r}(t) \} \right]$$

- $queue_{i,r}(t) = arr_{i,r}(t-1) - \frac{1}{T}(\hat{m}_{i,r} - m_{i,r}(t-1));$
- $m_{i,r}(t) = m_{i,r}(t-1) + T(arr_{i,r}(t-1) - r_i(t)) \leq \hat{m}_{i,r}$
- $r_i^\alpha(t) = r_i^\alpha(t-1) + \alpha_i(t) \frac{L_i}{T} (n_i k_{c,i} - k_i(t-1)) > 0$

Metering parameter

## Capacity constraints

$$\sum_{t=\tau}^{t_{end}} T \left\{ \sum_{i=1}^{rs} (\Delta q_i(t) - q_{c,i}) \right\} \leq 0$$

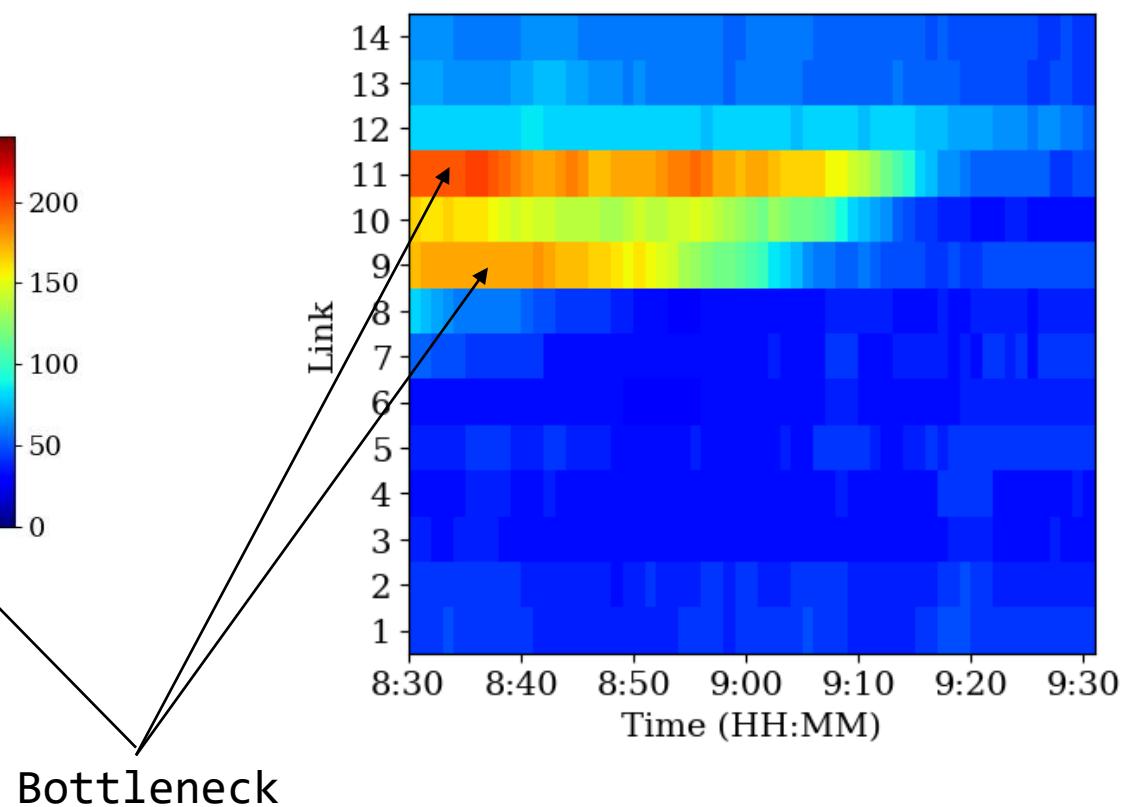
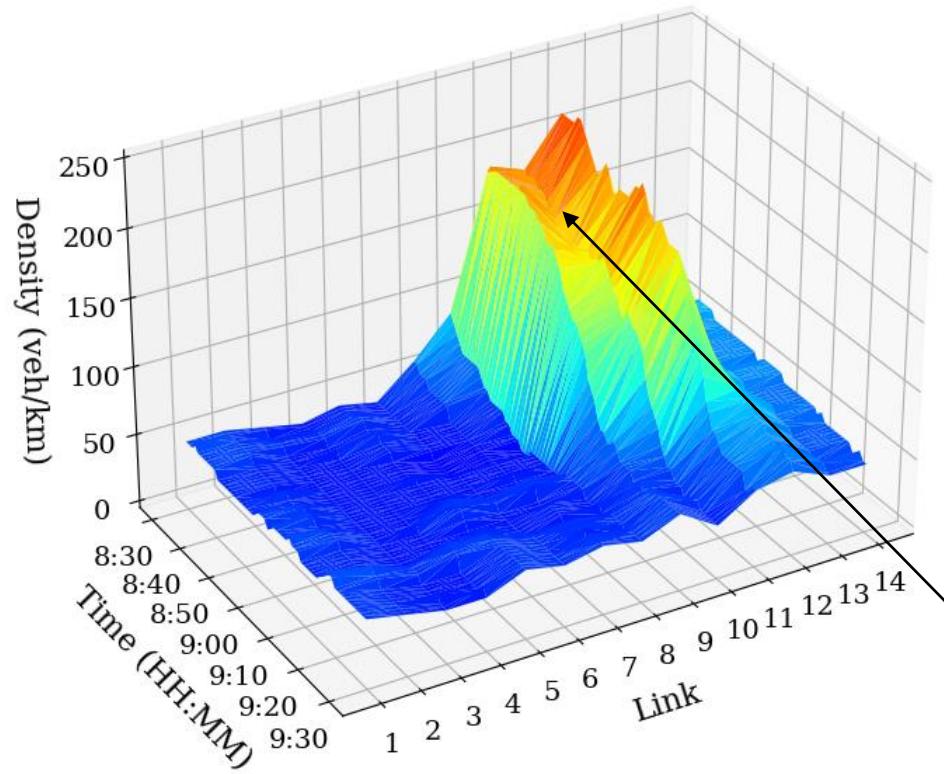


Green duration

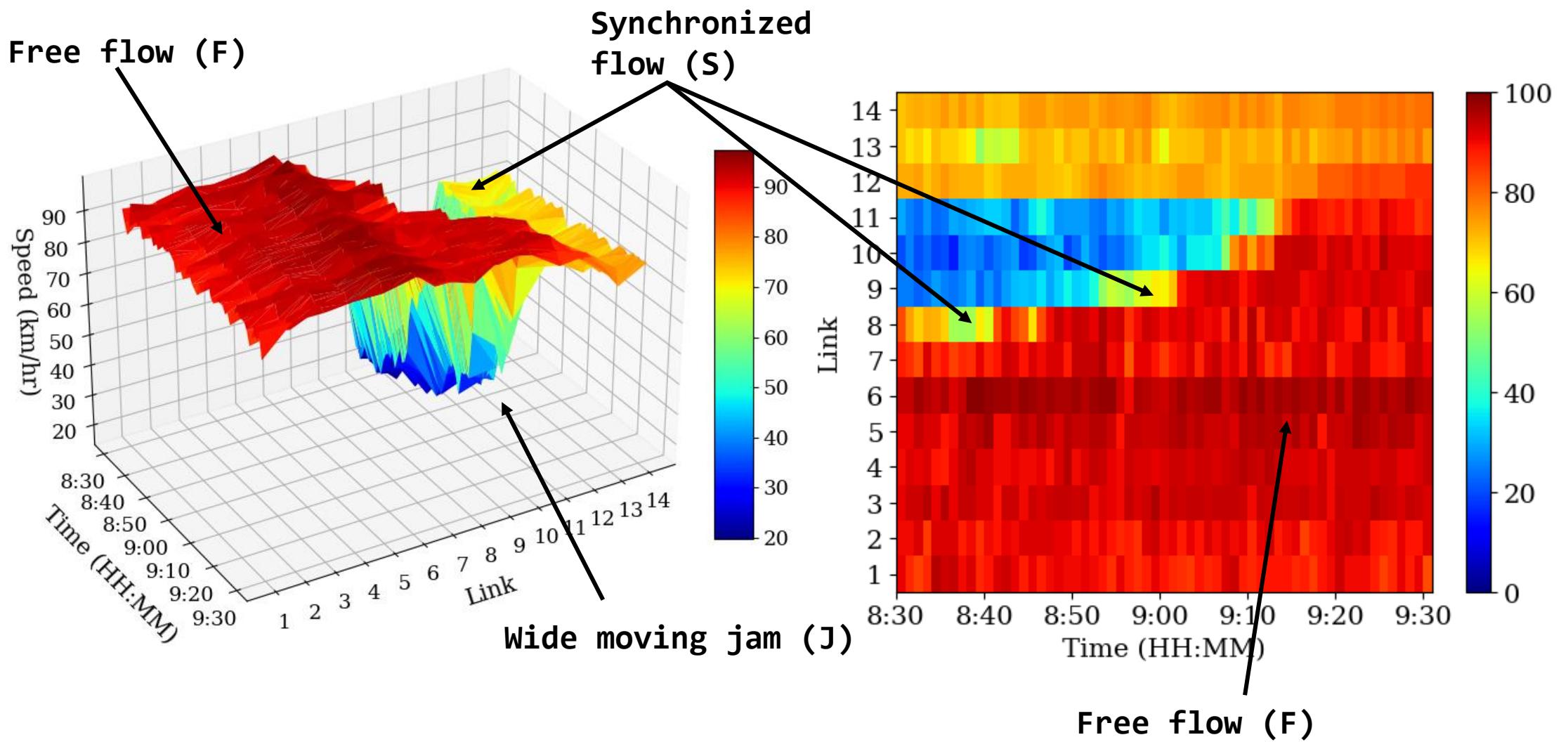
$$g_i(t) = \frac{r_i(t)}{r_s(t)} C_i$$

$$T = t_{record}/3600$$

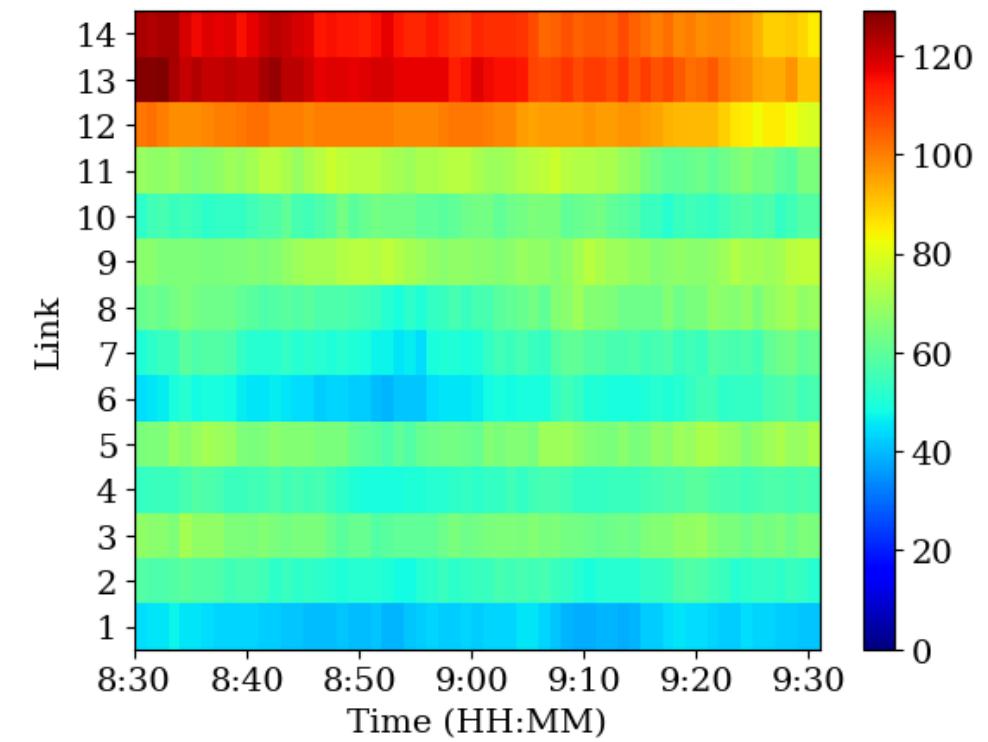
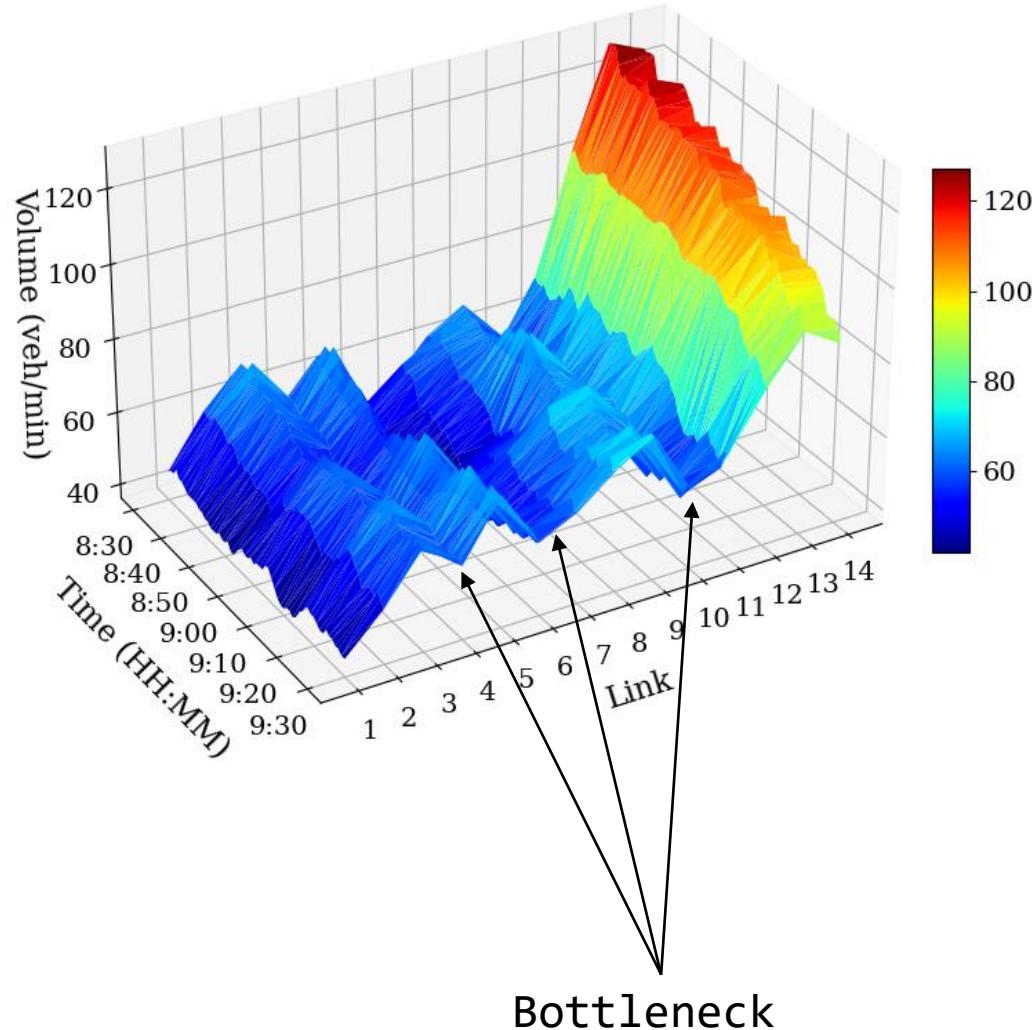
### (3) Computational Experiments



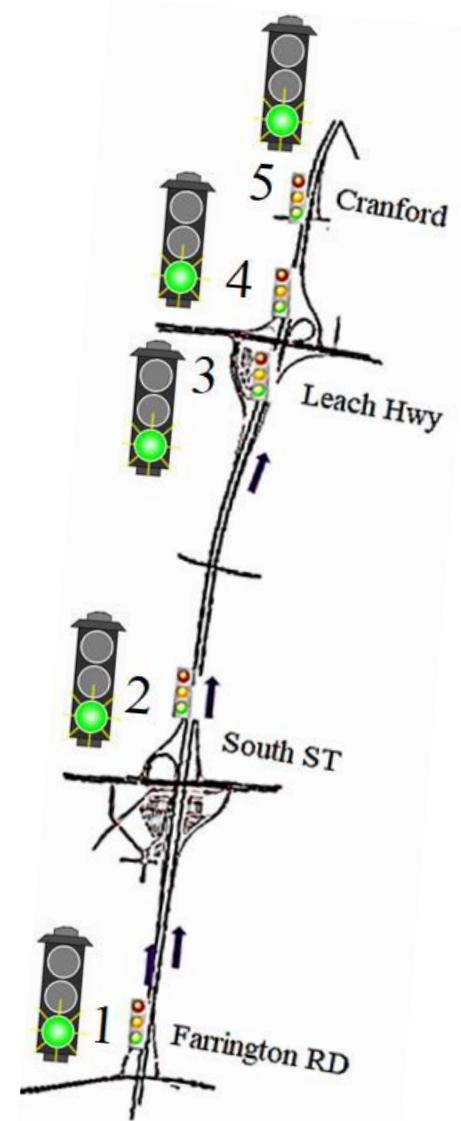
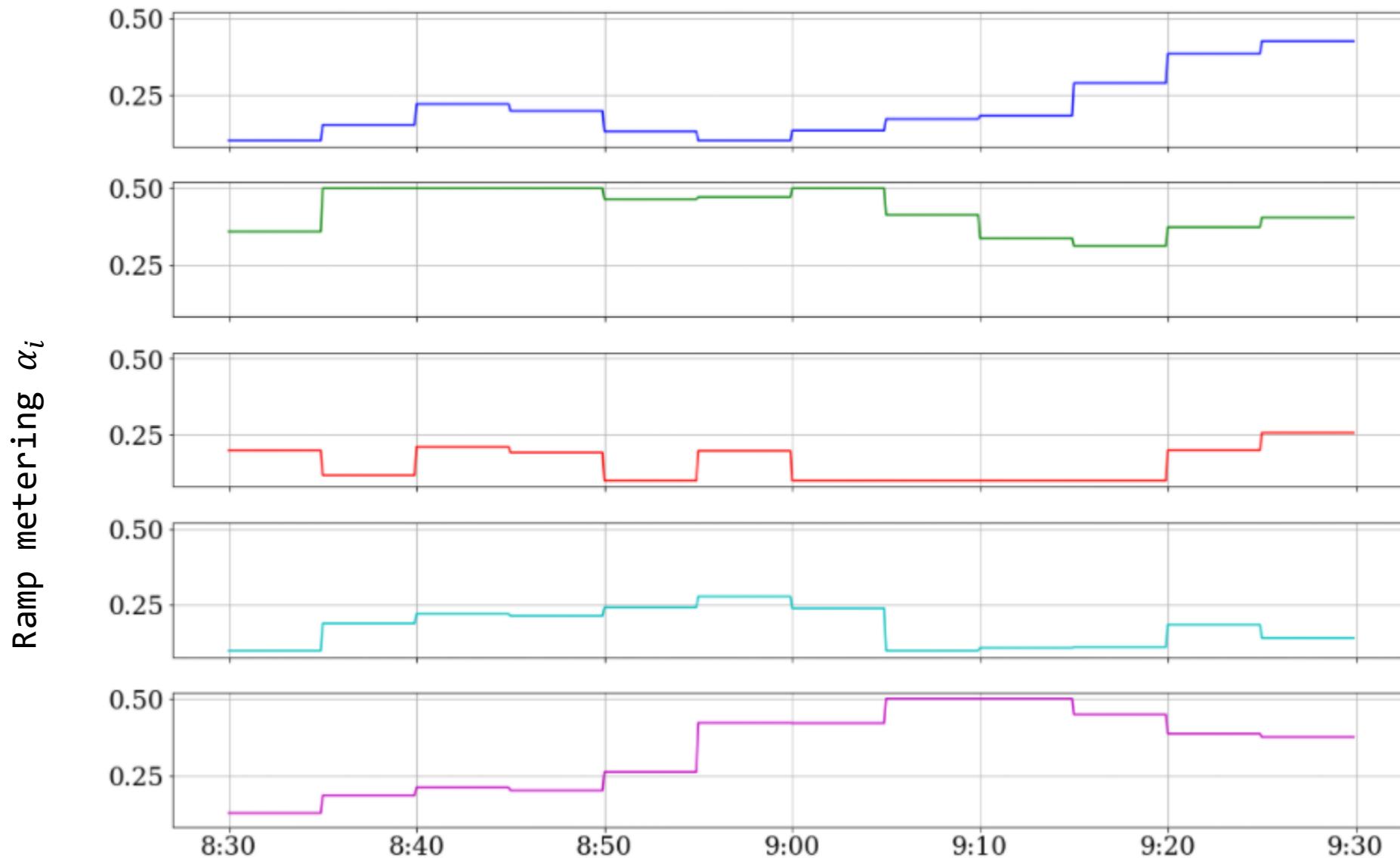
# Case I: Traffic speed (km / hr)



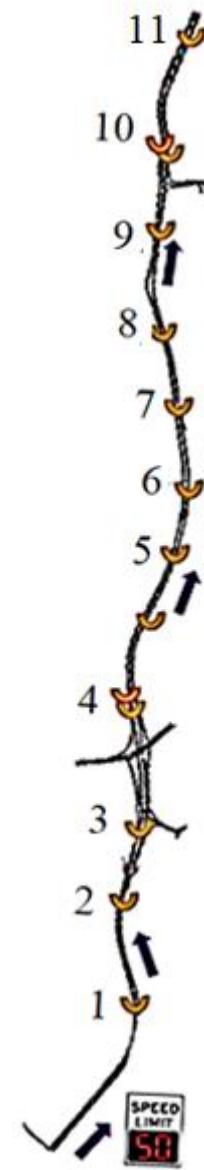
# Case I: Traffic flow rate (veh/min)



# Case I: RM

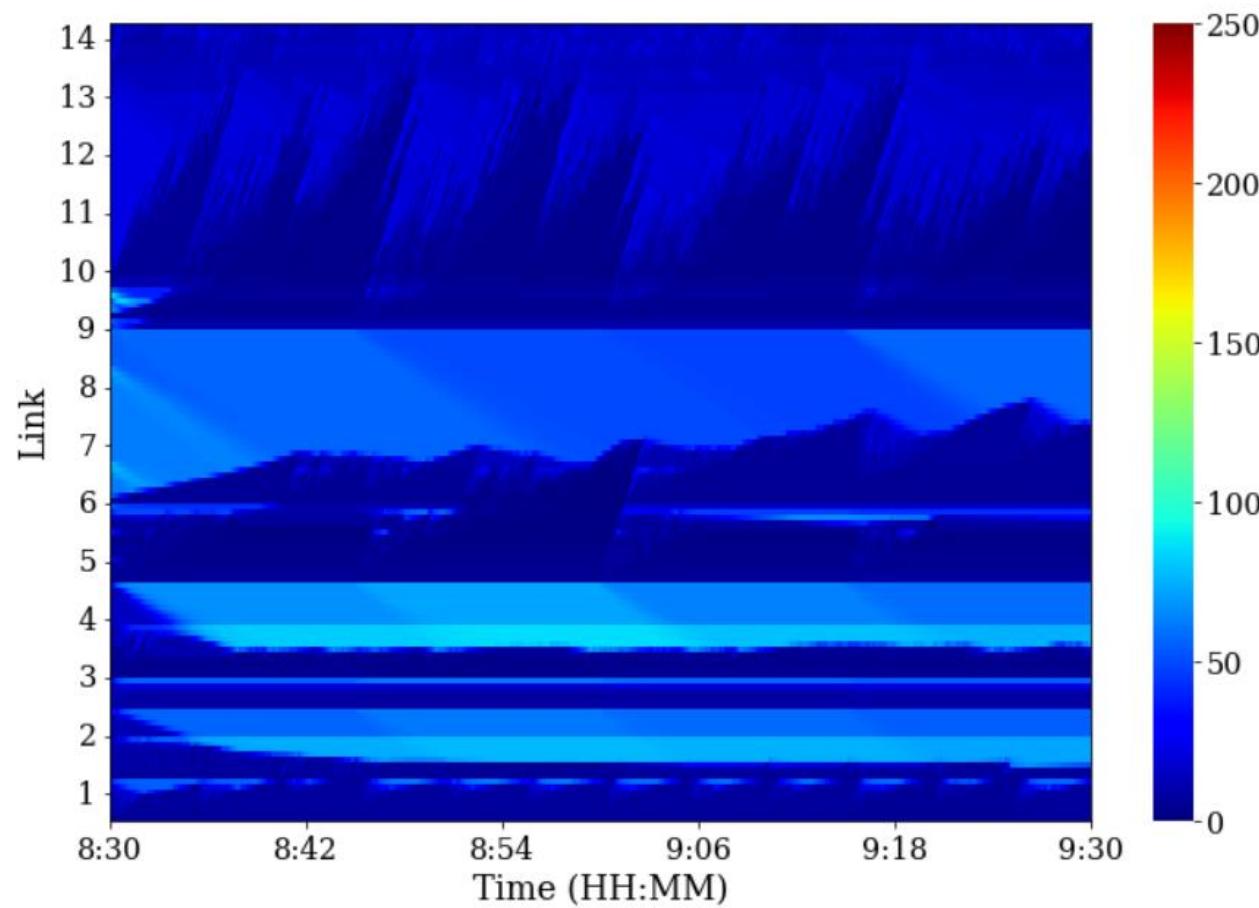


# Case I: VSL

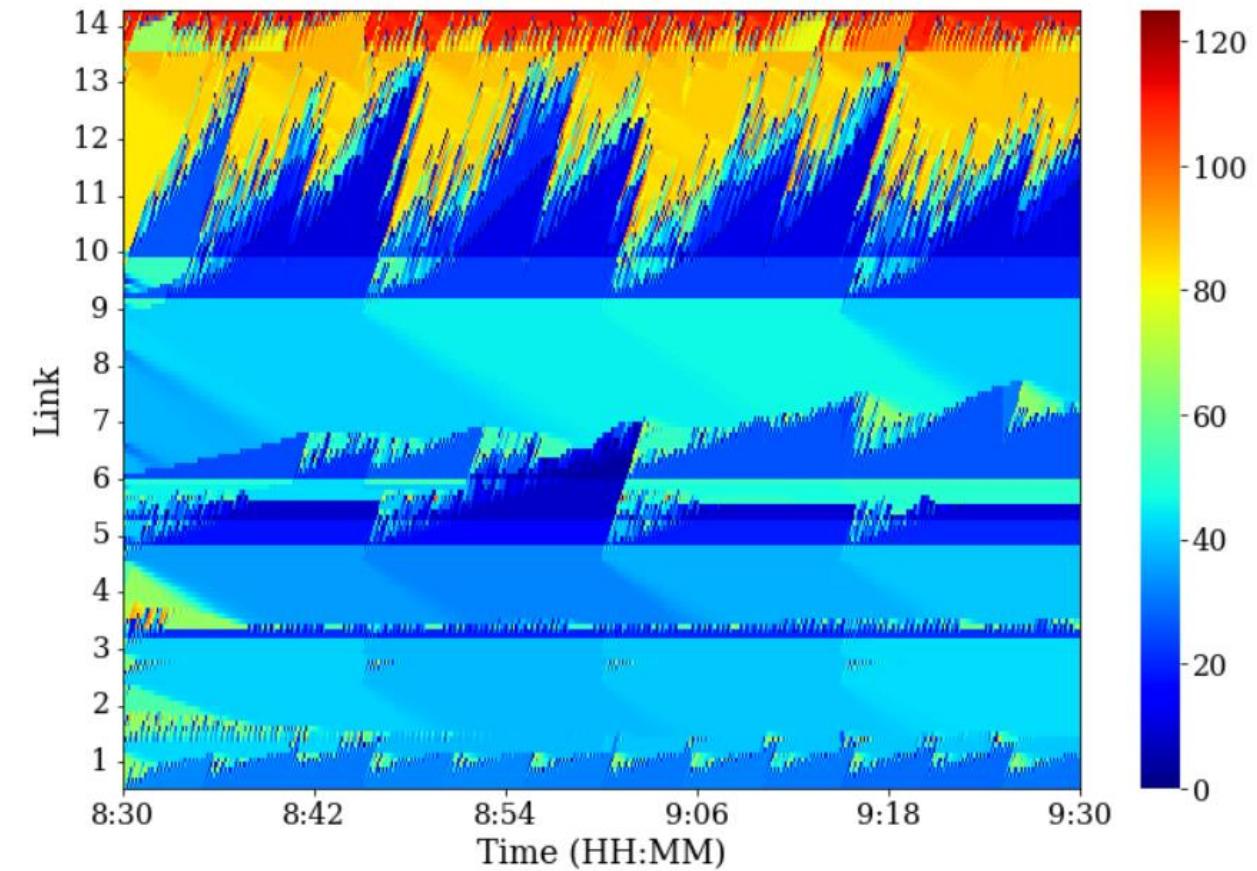


# Case I: Density and Flow rate

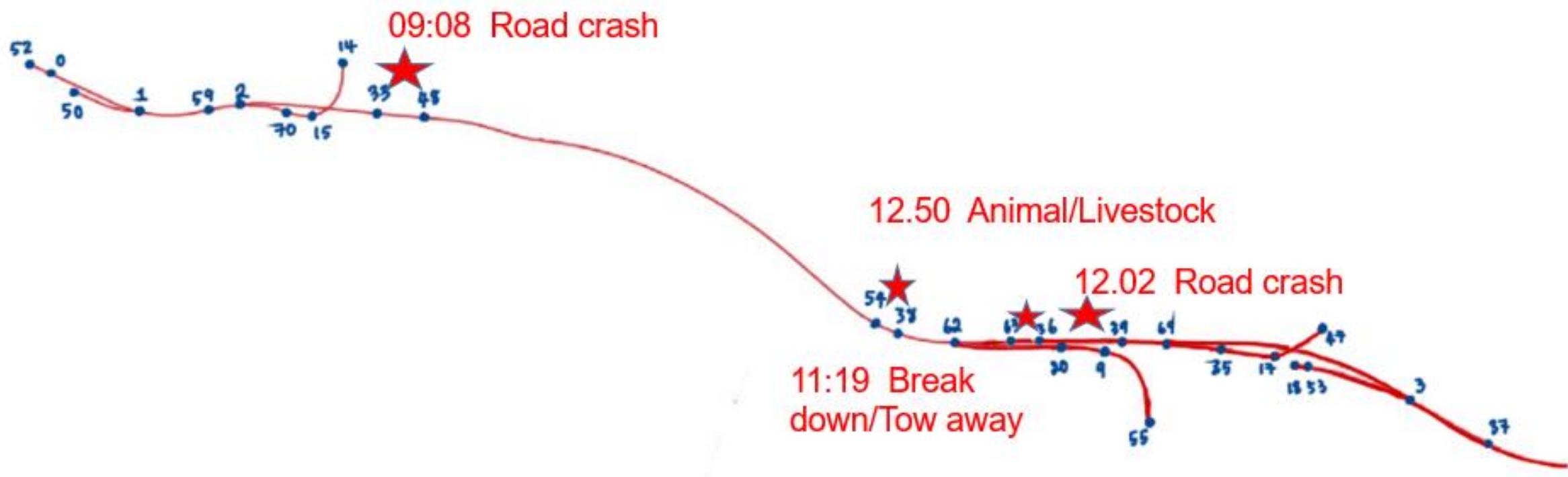
Density (veh/km)



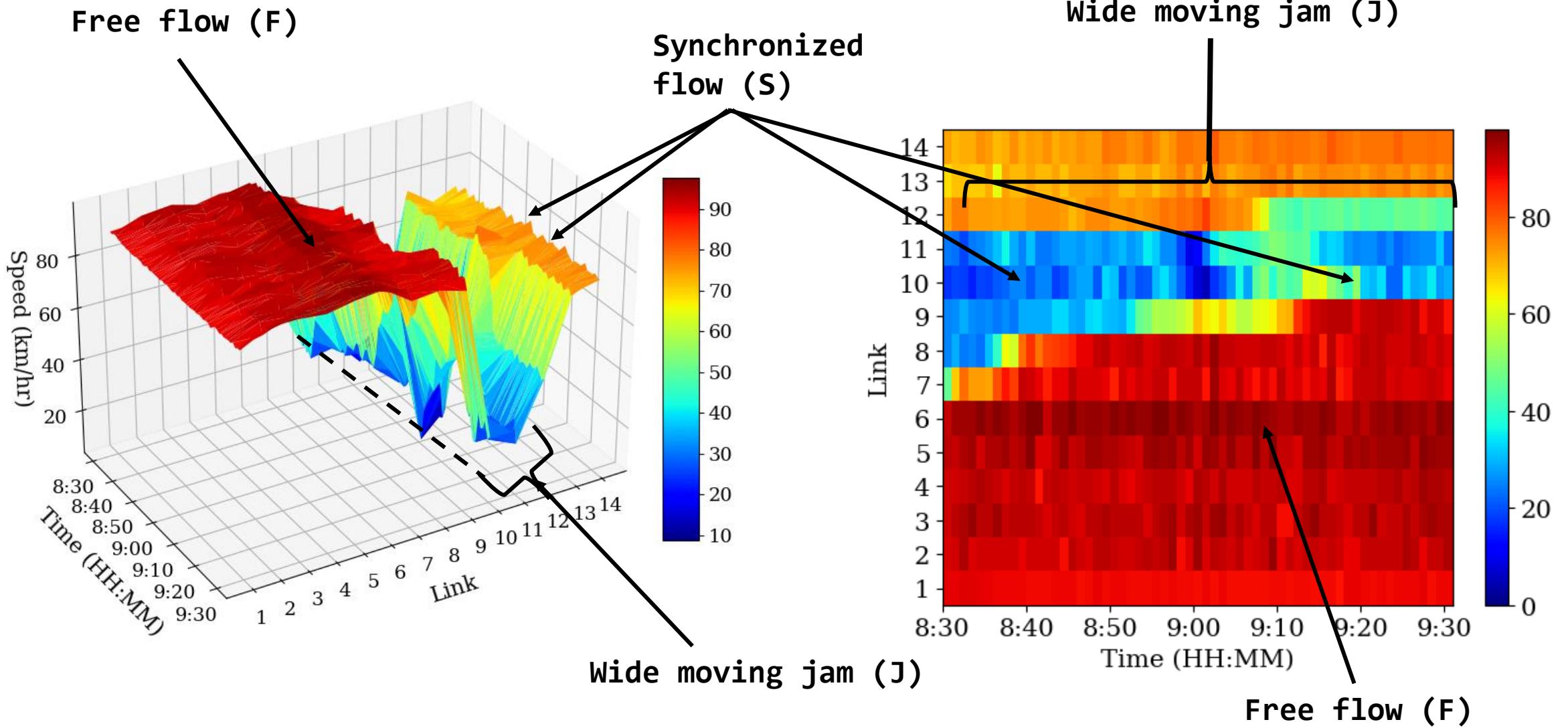
Flow rate (veh/min)



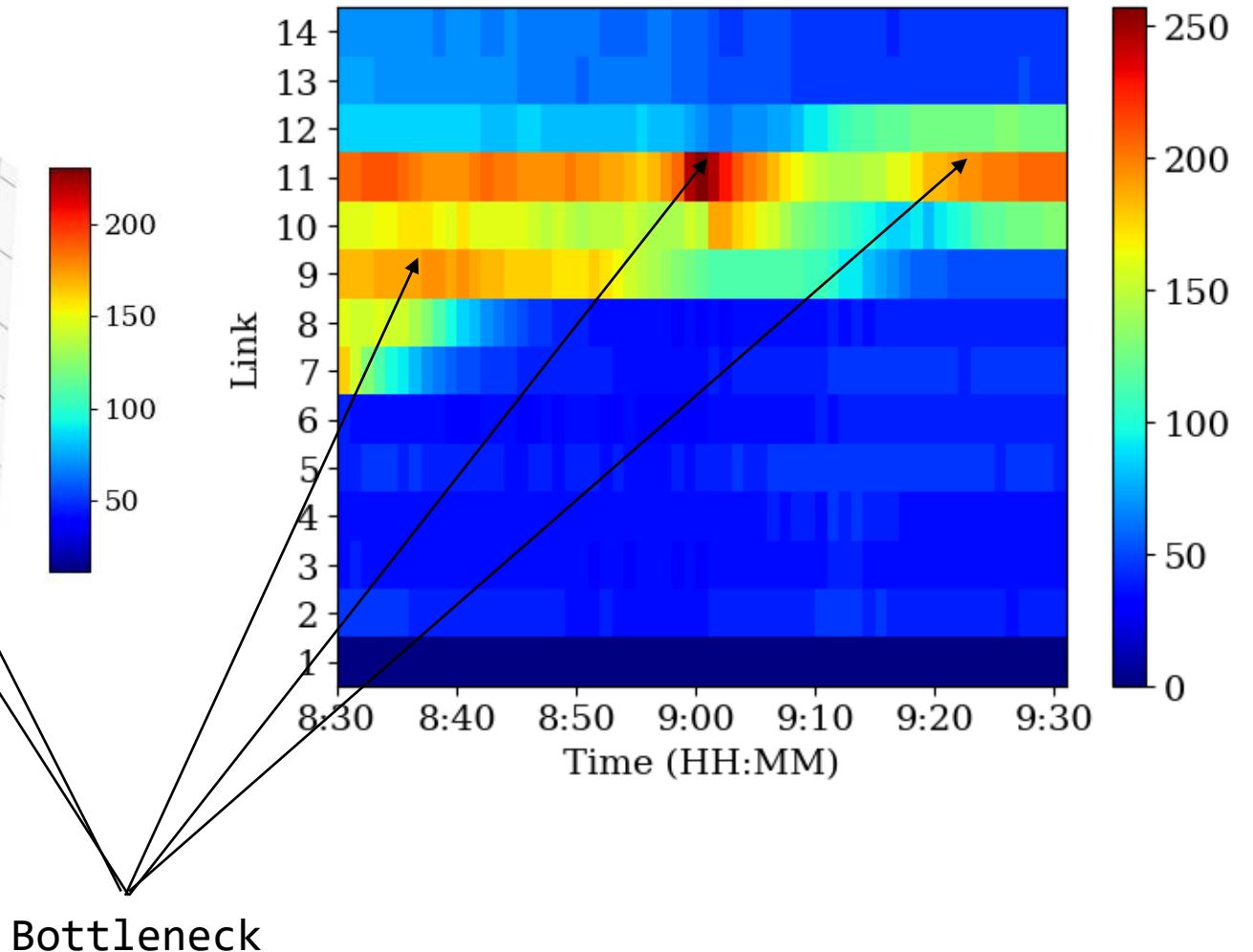
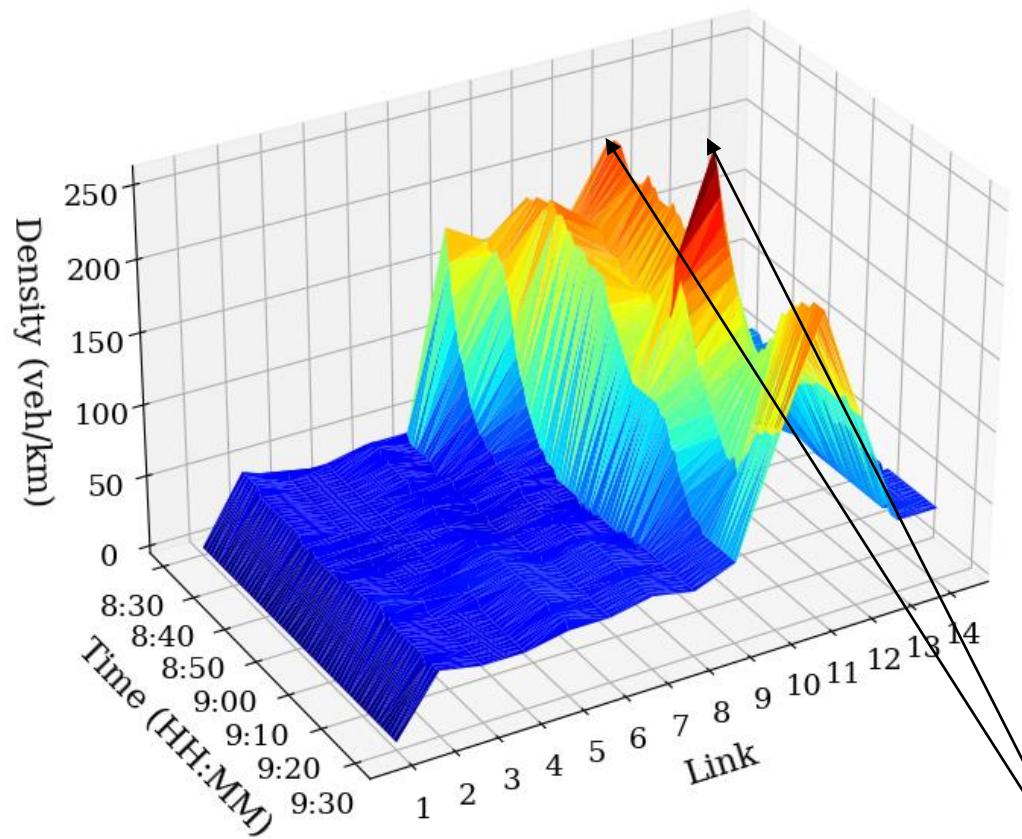
## Case II: With road incidents



## Case II: Traffic speed (km / hr)

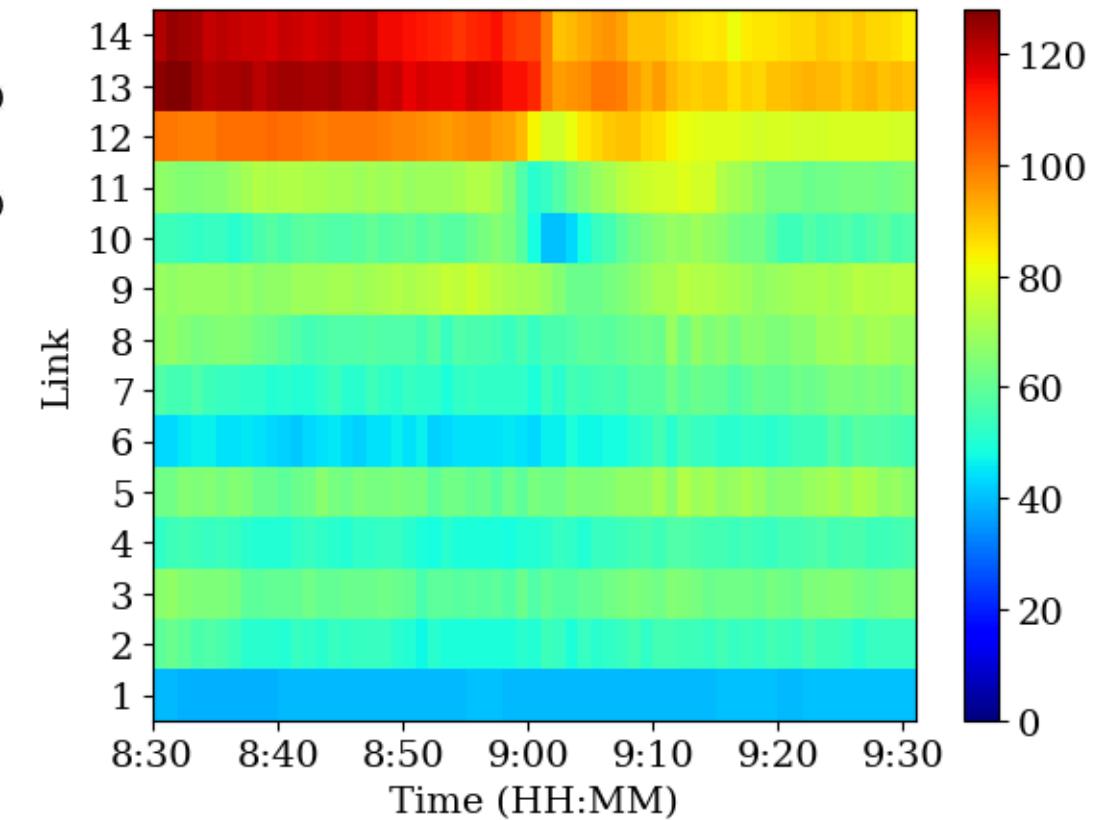
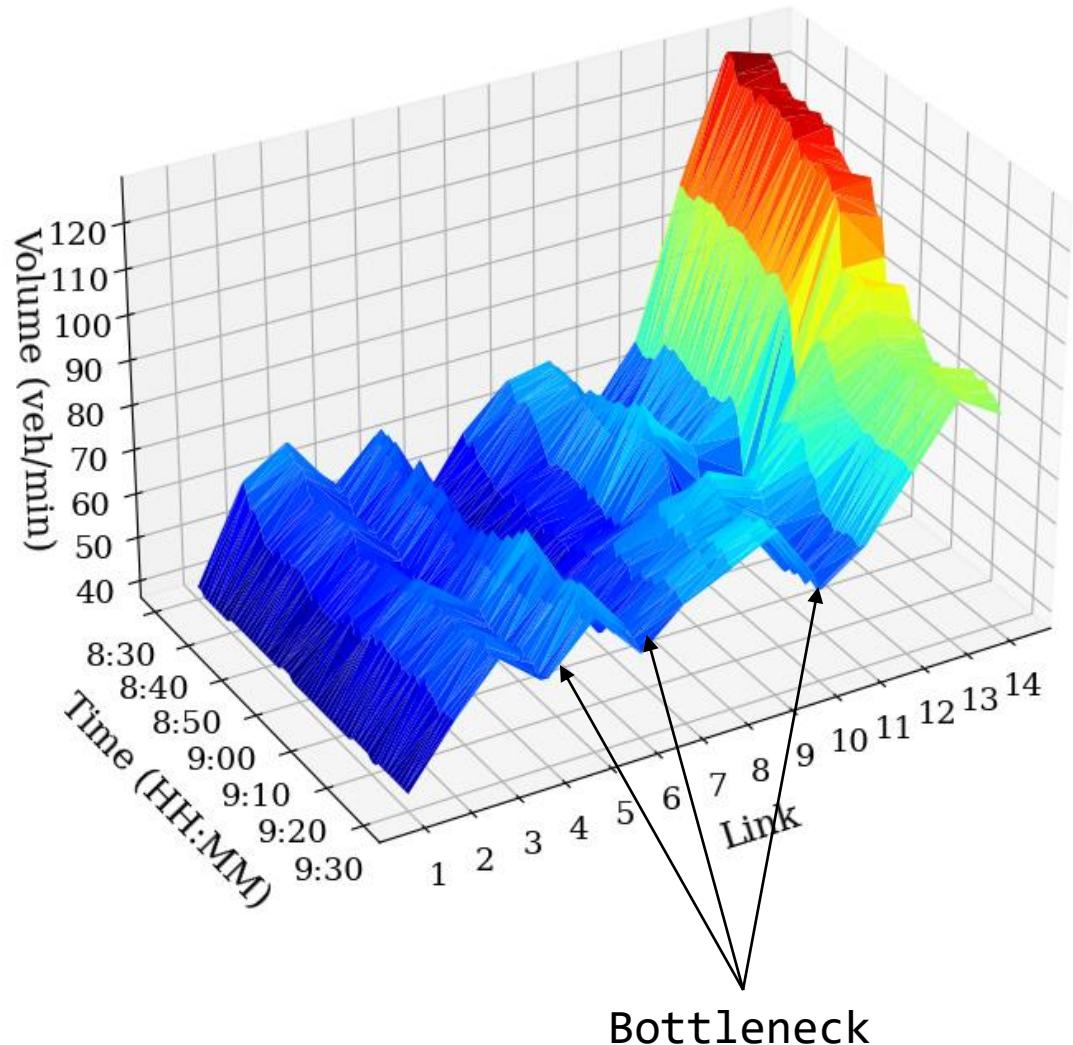


## Case II: Traffic density (veh / km)

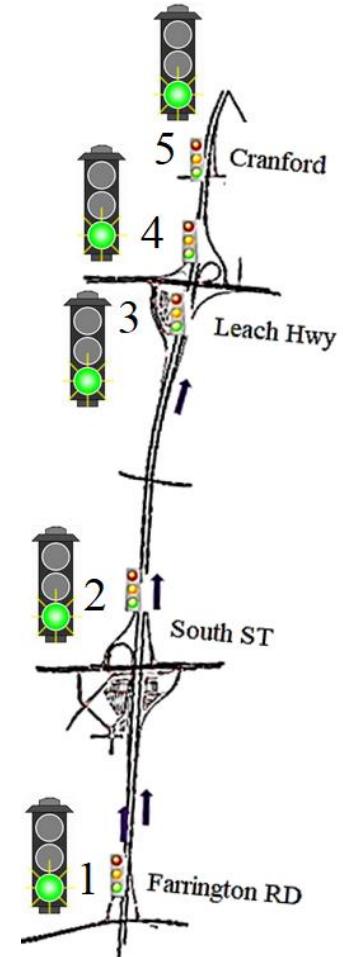
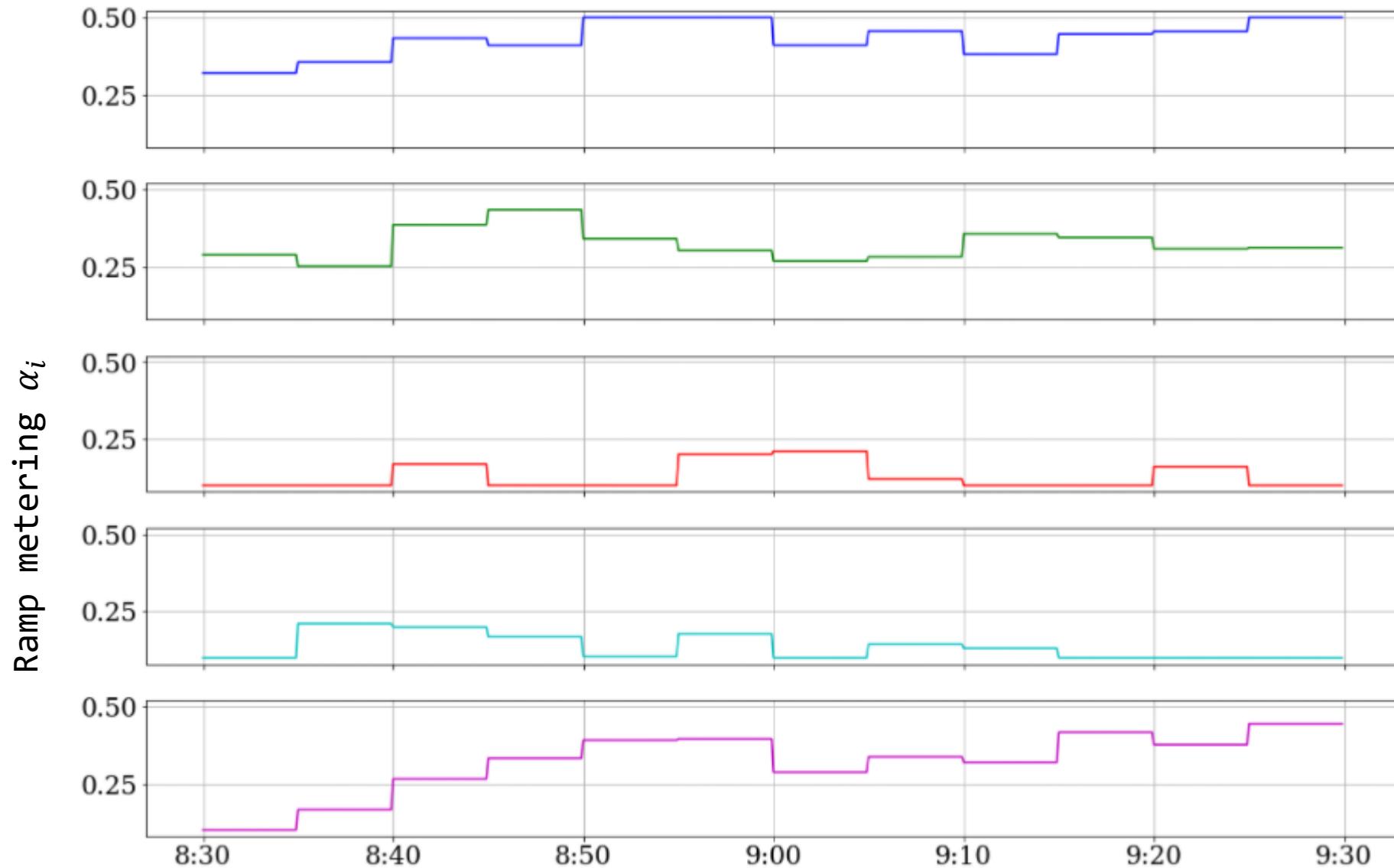


Bottleneck

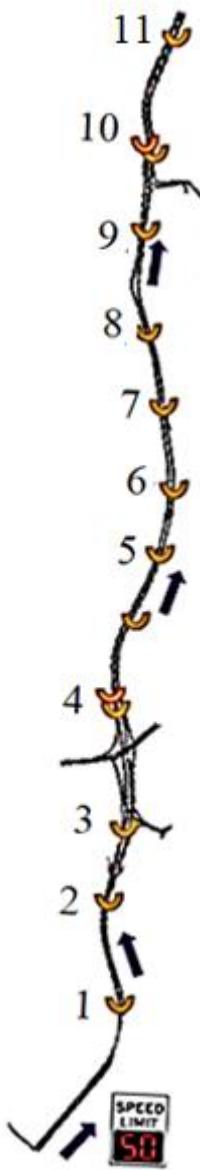
## Case II: Traffic flow rate (veh/min)



## Case II : RM

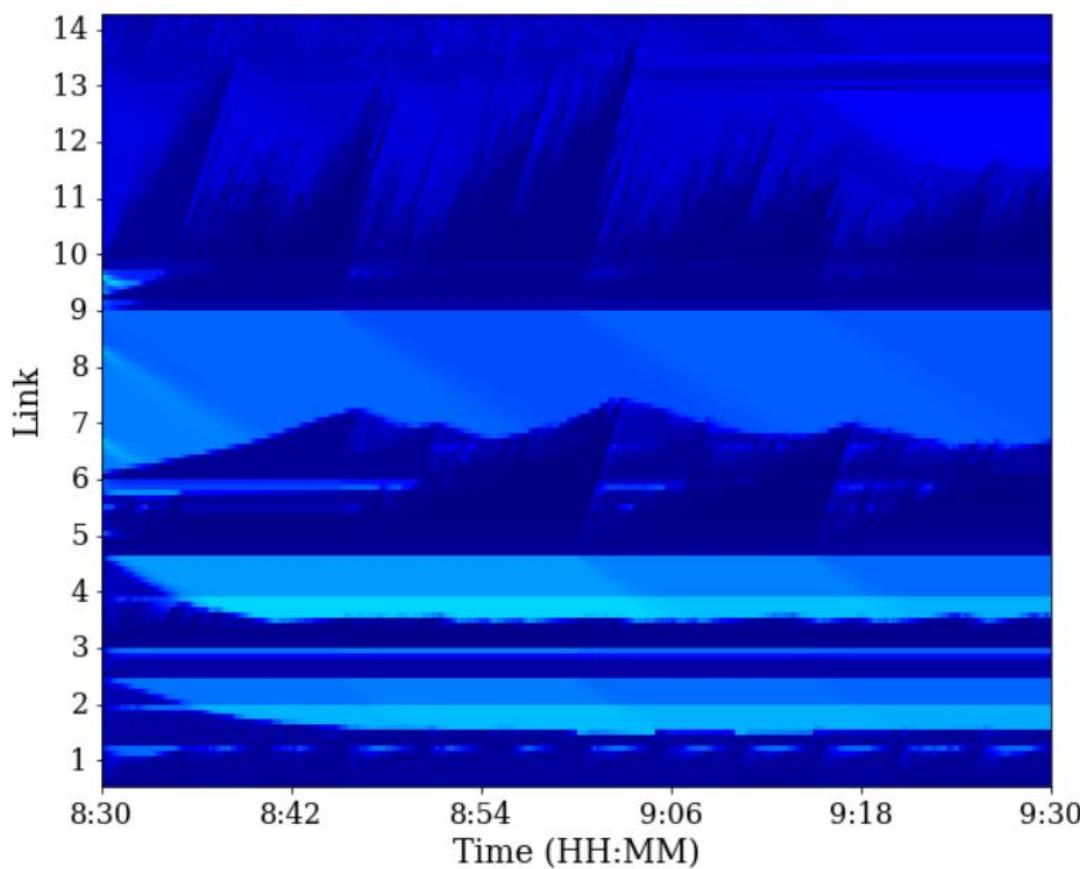


## Case II: VSL

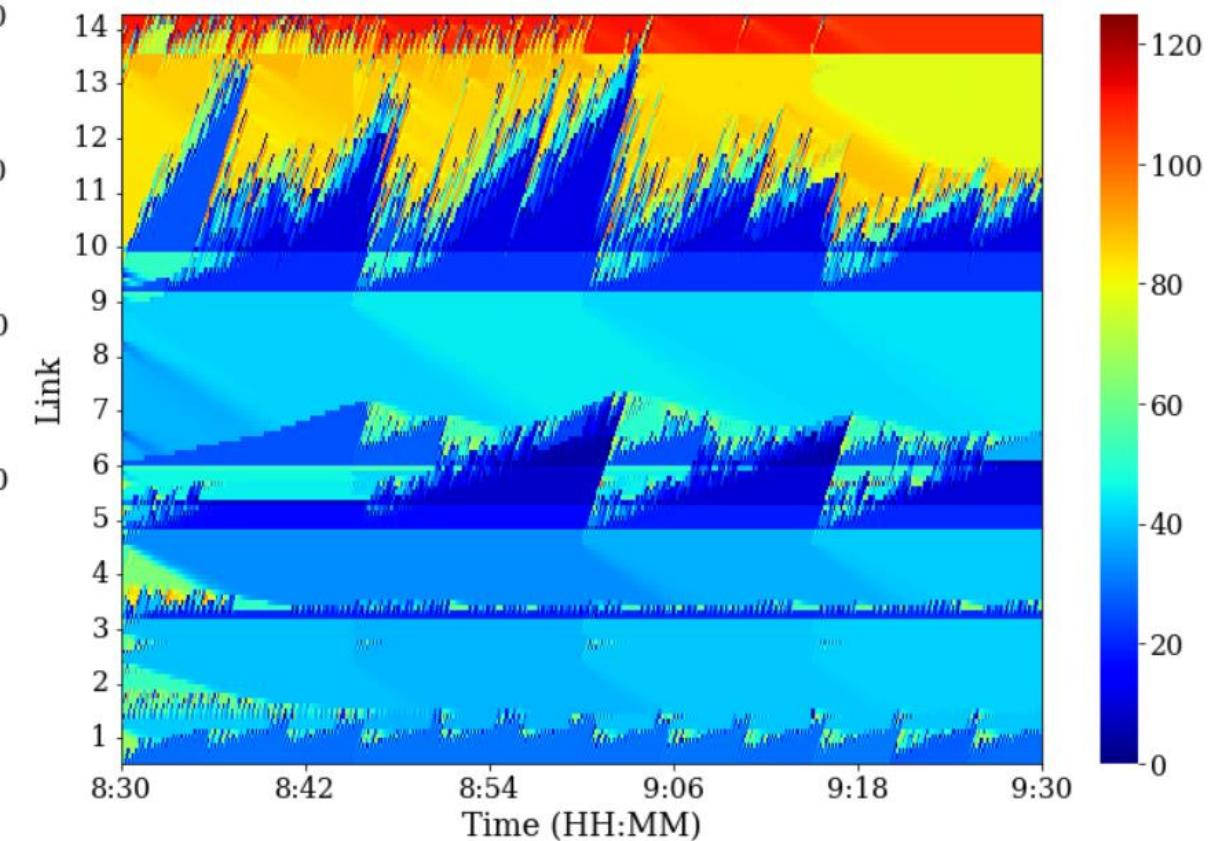


# Case II: Density and Flow rate

Density (veh/km)



Flow rate (veh/min)



## **2. Control of ramp metering Using Deep Koopman model**

PhD Student: C. Gu; Supervisors: YH Wu & B Wiwatanapataphee

# Model design

Dynamic system:

$$\begin{aligned} x_{t+1} &= f(x_t, u_t), \\ x_t &= [o_{t,l_1}, \dots, o_{t,l_L}, o_{t,m_M}, q_{t,j_1}, \dots, q_{t,j_J}]^\top, \\ u_t &= [a_{t,n_1}, \dots, a_{t,n_N}, d_{t,n_1}, \dots, d_{t,n_N}, d_{t,m_1}]^\top, \end{aligned} \quad (1)$$

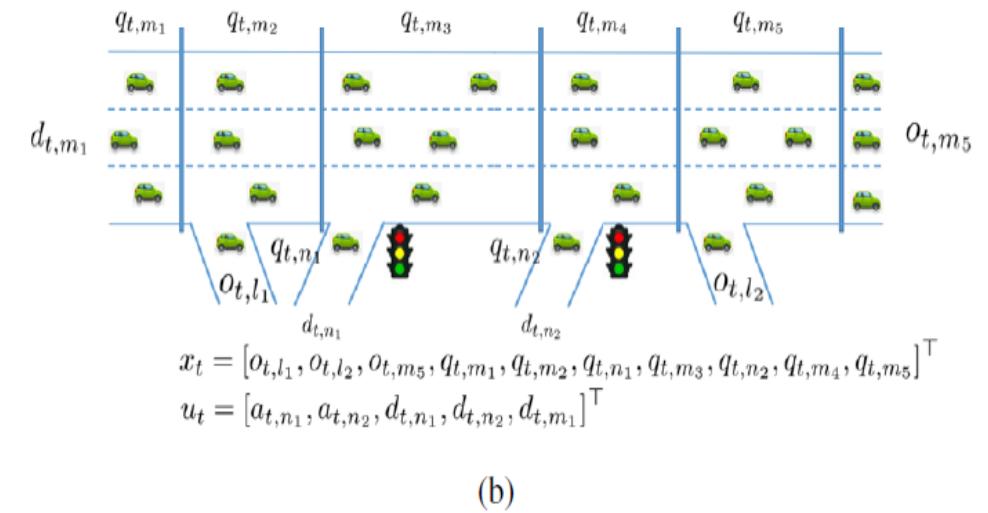
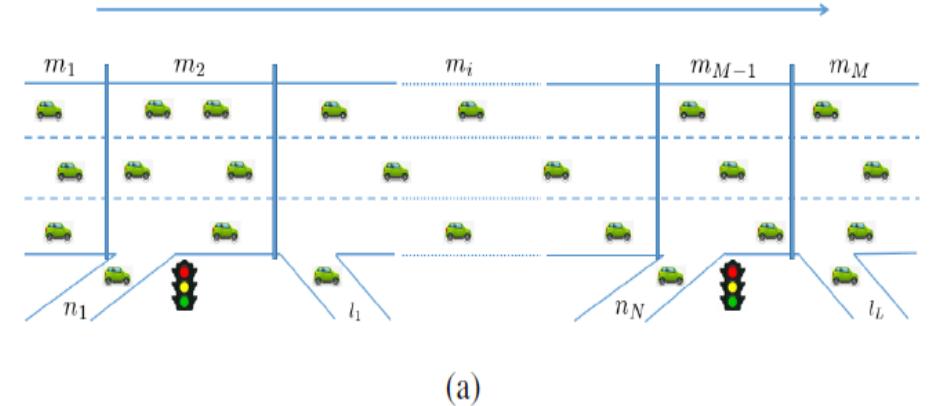
Optimization model:

$$\begin{aligned} \max_{u_t, t=0, \dots, T-1} \text{T} &= \sum_{t=0}^T v_t^\top x_t - \lambda \sum_{t=0}^{T-2} \|u_{t+1} - u_t\|^2, \\ \text{s.t.} \end{aligned} \quad (2)$$

$$x_{t+1} = f(x_t, u_t), t = 0, \dots, T-1, \quad (3)$$

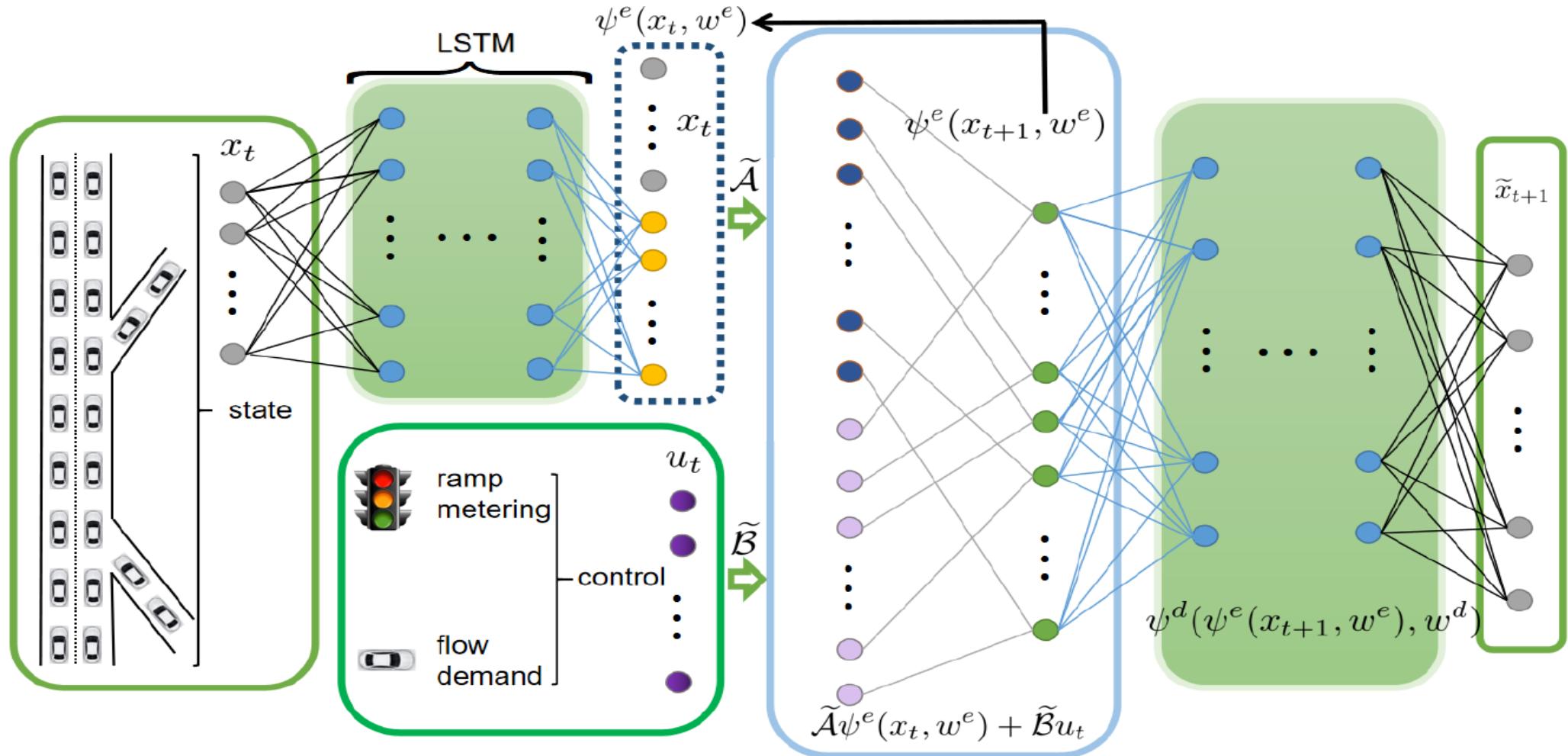
$$x_{min} \leq x_t \leq x_{max}, t = 0, \dots, T, \quad (4)$$

$$u_{min} \leq u_t \leq u_{max}, t = 0, \dots, T-1, \quad (5)$$



**Fig. 1:** Schematic diagram of ramp metering for a freeway (a) and an example of describing the state  $x_t$  and control  $u_t$  with ramp metering (b)

# Deep Koopman model



**Fig. 2:** The diagram of the proposed DKM. The original state  $x_t$  is lifted with the encoder, i.e.,  $\psi^e(x_t, w^e)$ . Then  $\psi^e(x_t, w^e)$ ,  $u_t$  forms the lifted state for constructing the linear evolution in the vector-valued observables. The freeway traffic flow dynamics can be recovered via a decoder  $\psi^d(\psi^e(x_{t+1}, w^e), w^d)$  from the vector-valued observables

$$x_{t+1} = f(x_t, u_t).$$



$$\begin{aligned}\psi^e(x_{t+1}) &= \tilde{\mathcal{A}}\psi^e(x_t, w^e) + \tilde{\mathcal{B}}u_t \\ \tilde{x}_t &= \psi^d(\psi^e(x_t, w^e), w^d).\end{aligned}$$

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**Algorithm 2** The Deep Koopman Method (DKM)

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- 1: Initialization:  $w^e, w^d, \tilde{\mathcal{A}}, \tilde{\mathcal{B}}, M, Epoch = 0, Epoch_{max}, \alpha_i, i = 1, \dots, 5$ , batch size  $b_s$ , a small constant  $\epsilon > 0$ ;
- 2: Train: trained  $w^e, w^d, \tilde{\mathcal{A}}$  and  $\tilde{\mathcal{B}}$ ;
- 3: **while**  $Epoch > Epoch_{max}$  or  $|L| \leq \epsilon$  **do**
- 4:     Reset the training episodes;
- 5:     **while** Epoch is not Terminated **do**
- 6:         Sample a batch data sequences of state  $x$  and control  $u$ ;
- 7:         Compute the vector-valued observables  $\psi^e(x, w^e)$  with (18) and reconstruction states  $\tilde{x} = \psi^d(\psi^e(x, w^e), w^d)$  with (20);
- 8:         Calculate the multi-step vector-valued observables  $A^l \Phi(x_0, w^e, u_0)$  with (22) and predicted states  $\tilde{x}_l = \psi^d(A^l \Phi(x_0, w^e, u_0), w^d)$ , where  $l = 1, 2, \dots, M$ ;
- 9:         Compute the loss function  $L$  with (26);
- 10:         Update  $w^e, w^d, \tilde{\mathcal{A}}$  and  $\tilde{\mathcal{B}}$  via solving problem (26);
- 11:     **end while**
- 12:      $Epoch = Epoch + 1$
- 13: **end while**

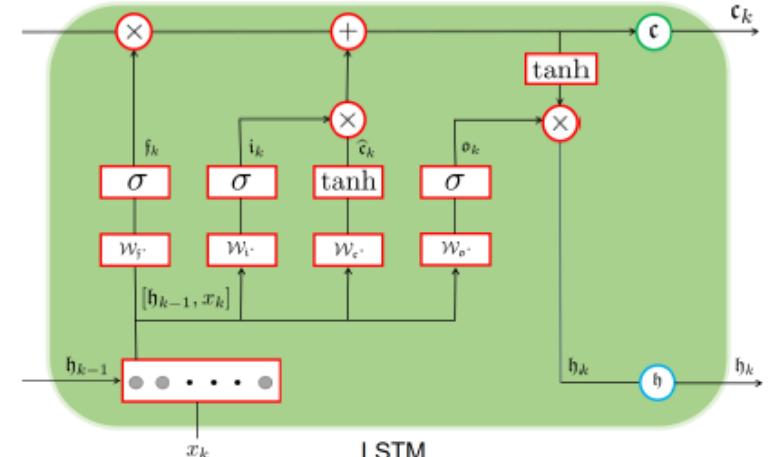


Fig. 3: The diagram of the LSTM

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**Algorithm 1** : Compute the output sequence of an LSTM network

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- 1: Input: Sequence  $x_1, x_2, \dots, x_K$ ,
- 2: Output: Sequence  $h_1, h_2, \dots, h_K$ ,
- 3: Set  $h_0 = 0$
- 4: Set  $c_0 = 0$
- 5: **for**  $k \leftarrow k$  to  $K$  **do do**
- 6:      $f_k = \sigma(W_f[h_{k-1}, x_k] + b_f)$
- 7:      $i_k = \sigma(W_i[h_{k-1}, x_k] + b_i)$
- 8:      $\hat{c}_k = \tanh(W_c[h_{k-1}, x_k] + b_c)$
- 9:      $c_k = f_k \otimes c_{k-1} + i_k \otimes \hat{c}_k$
- 10:      $o_k = \sigma(W_o[h_{k-1}, x_k] + b_o)$
- 11:      $h_k = o_k \otimes \tanh(c_k)$
- 12: **end for**

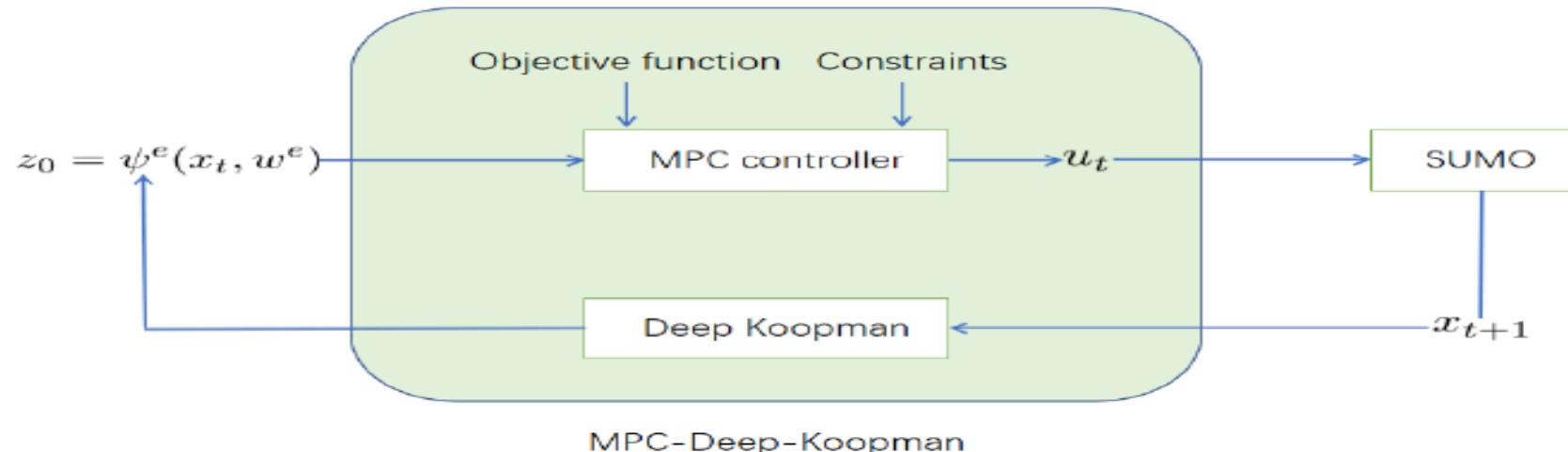
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**Algorithm 3** : MPC-Deep-Koopman to compute the control sequence of Problem T

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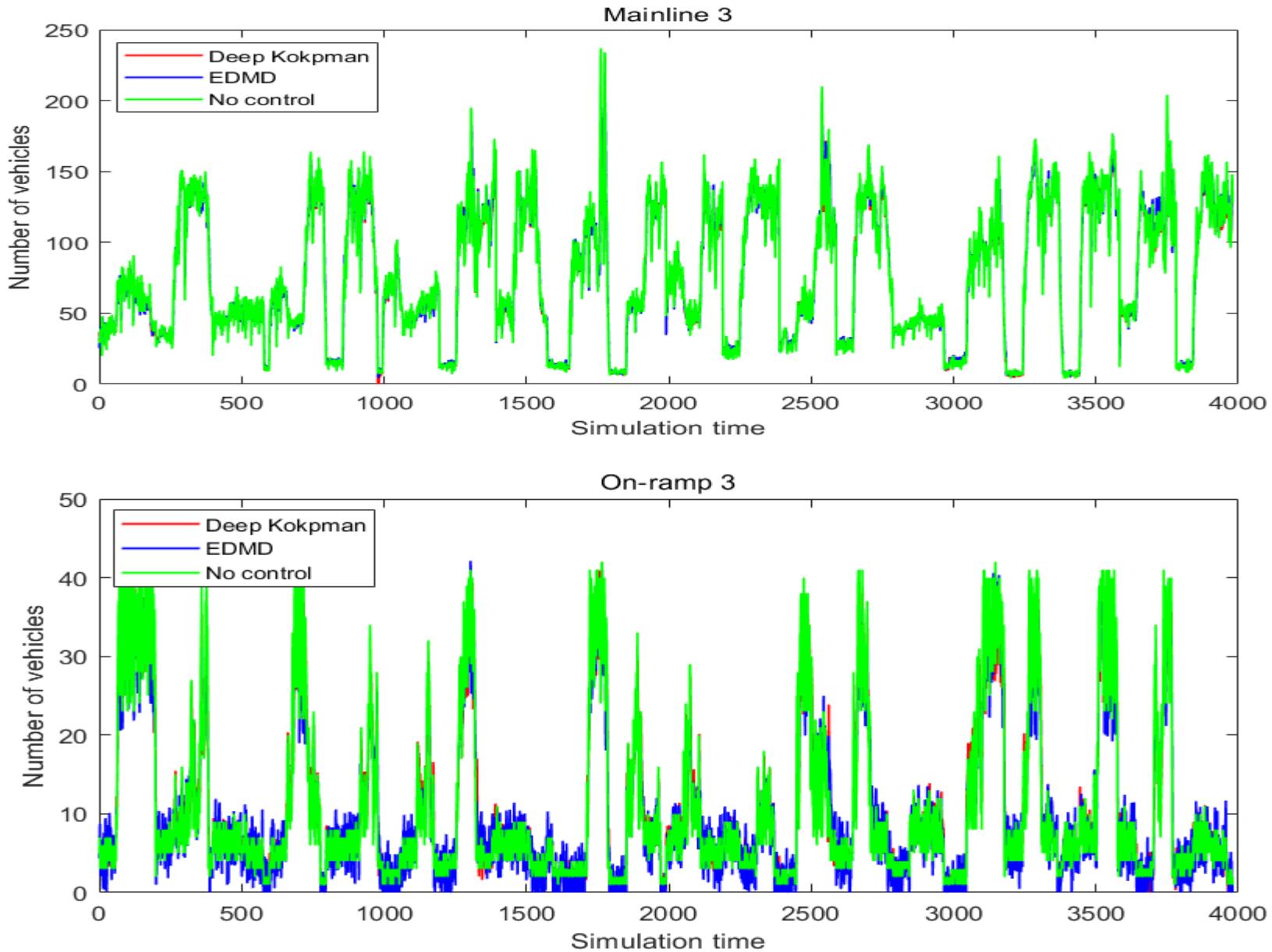
```
1: for  $t = 0, 1, \dots, T$  do
2:   Let  $z_0 = \psi^e(x_t, w^e)$ ;
3:   Minimize Problem T to obtain an optimal solution  $U^*$ ;
4:   Let  $u_t = U^*(1 : m)$ ;
5:   Update  $\tilde{x}_{t+1}$  with system (28).
6:   Obtain practical  $x_{t+1}$  with SUMO by implementing
   the control  $u_t$ .
7: end for
```

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**Fig. 4:** The diagram of MPC-Deep-Koopman to compute the control sequence

# Result

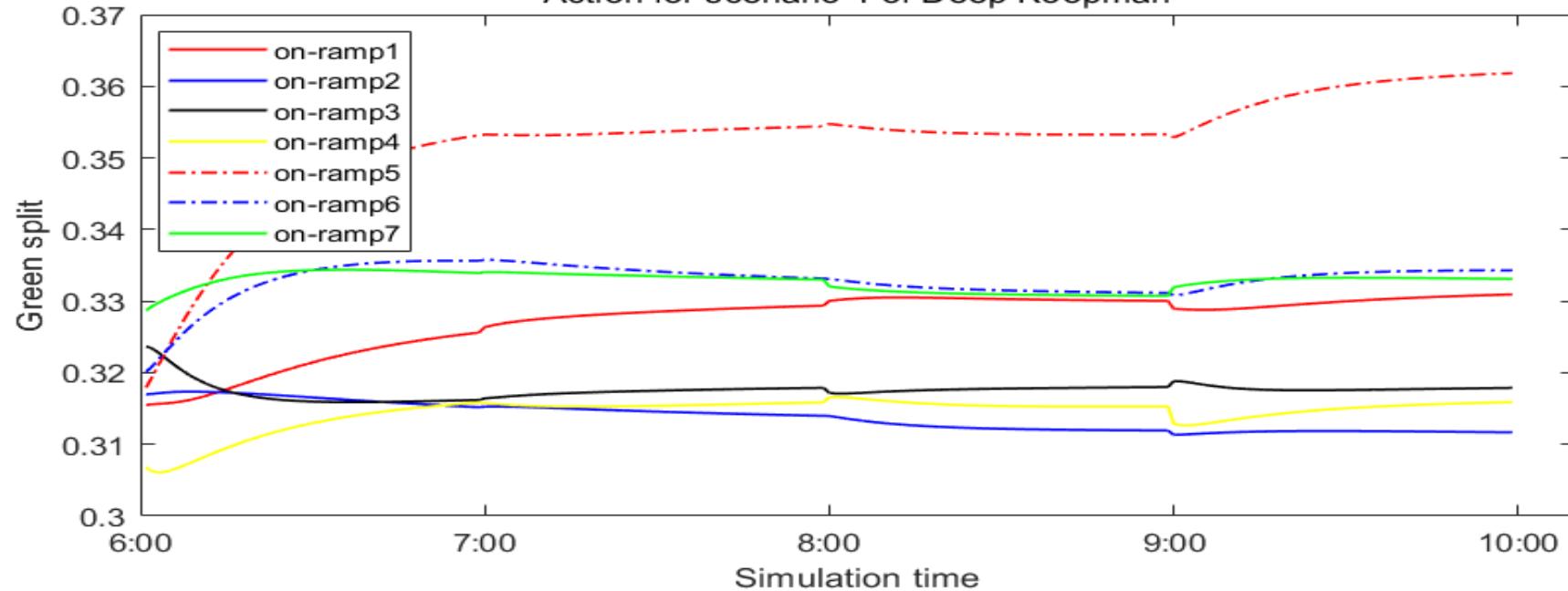


The Comparison of State Prediction between EDMD and the proposed Deep Koopman for Scenario 1

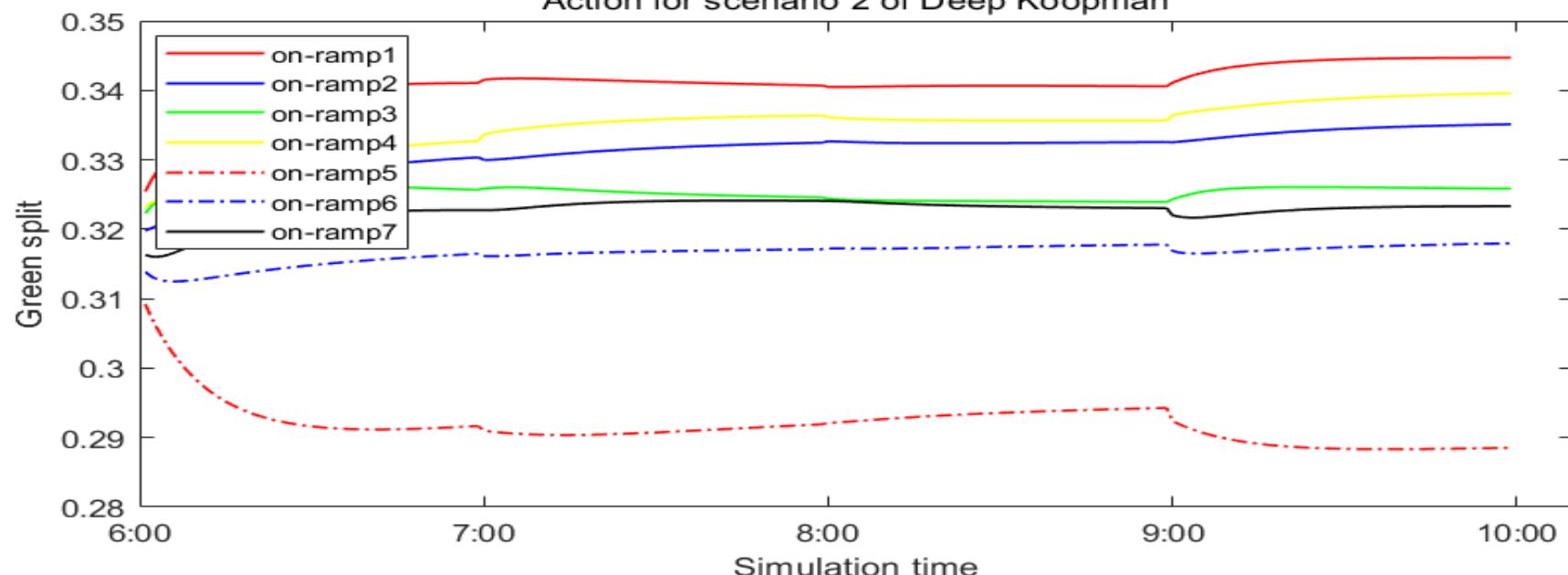


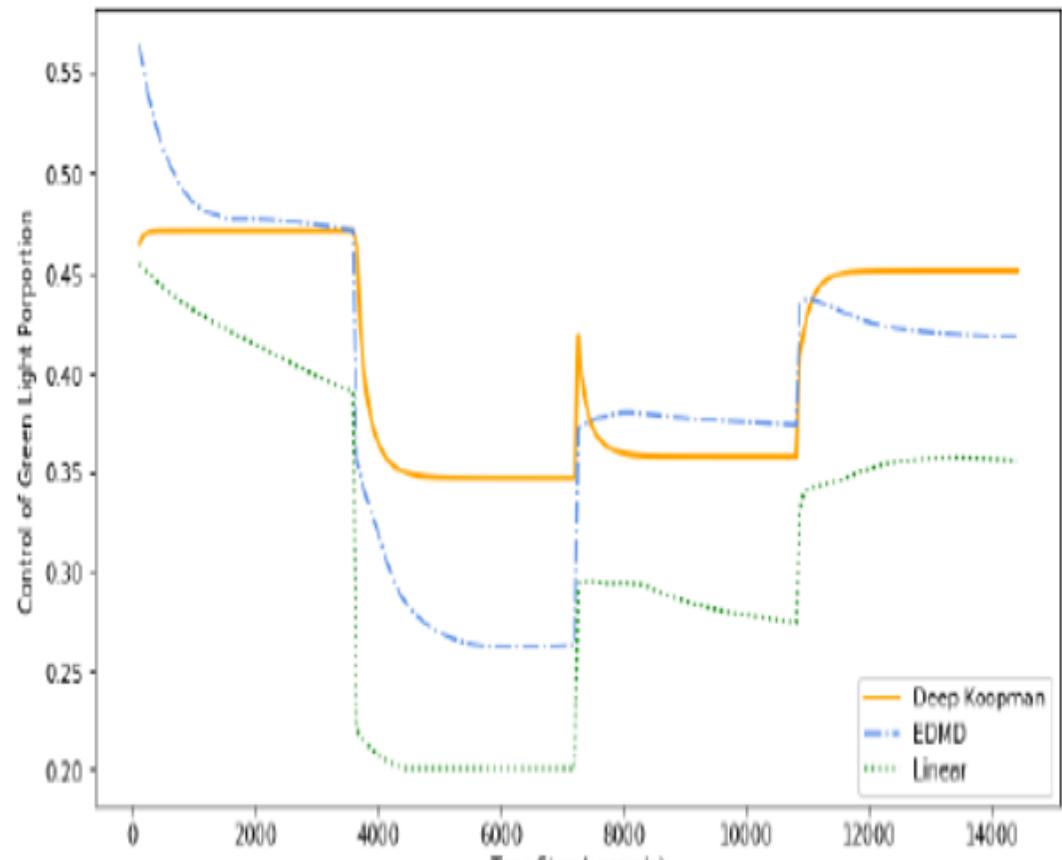
The Comparison of Number of Leaving Vehicles between baseline approaches and the proposed Deep Koopman Method

Action for scenario 1 of Deep Koopman

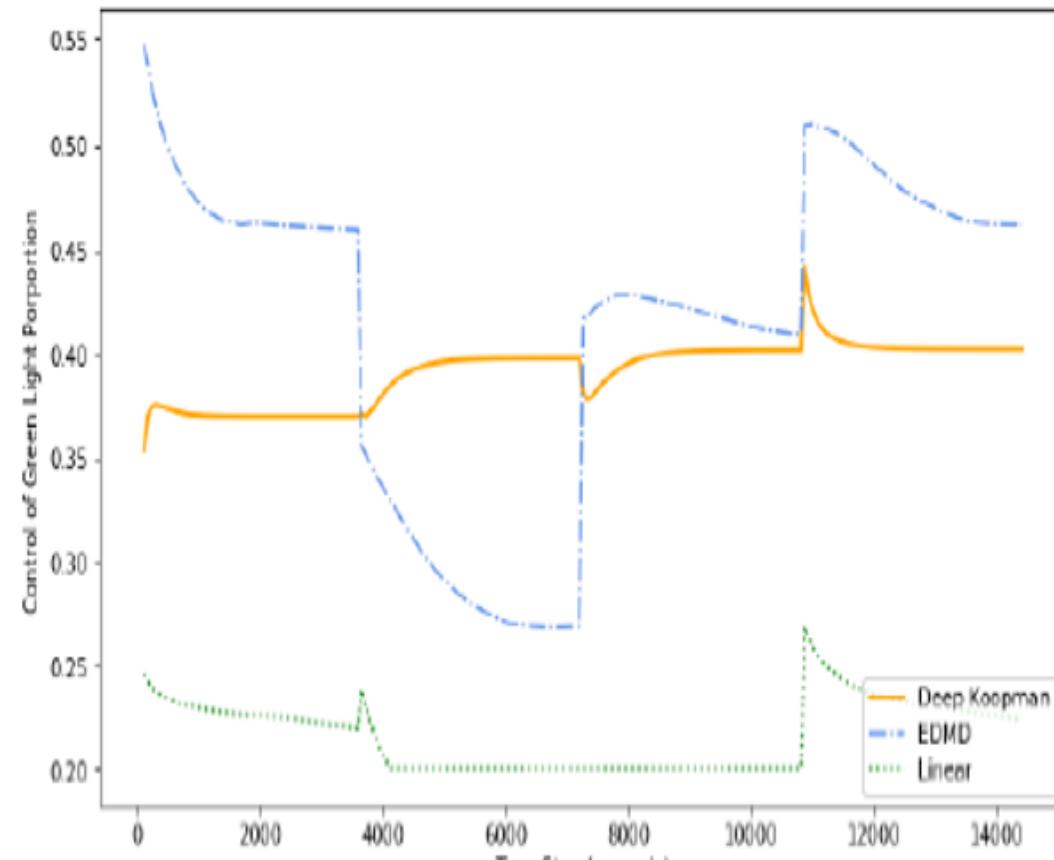


Action for scenario 2 of Deep Koopman



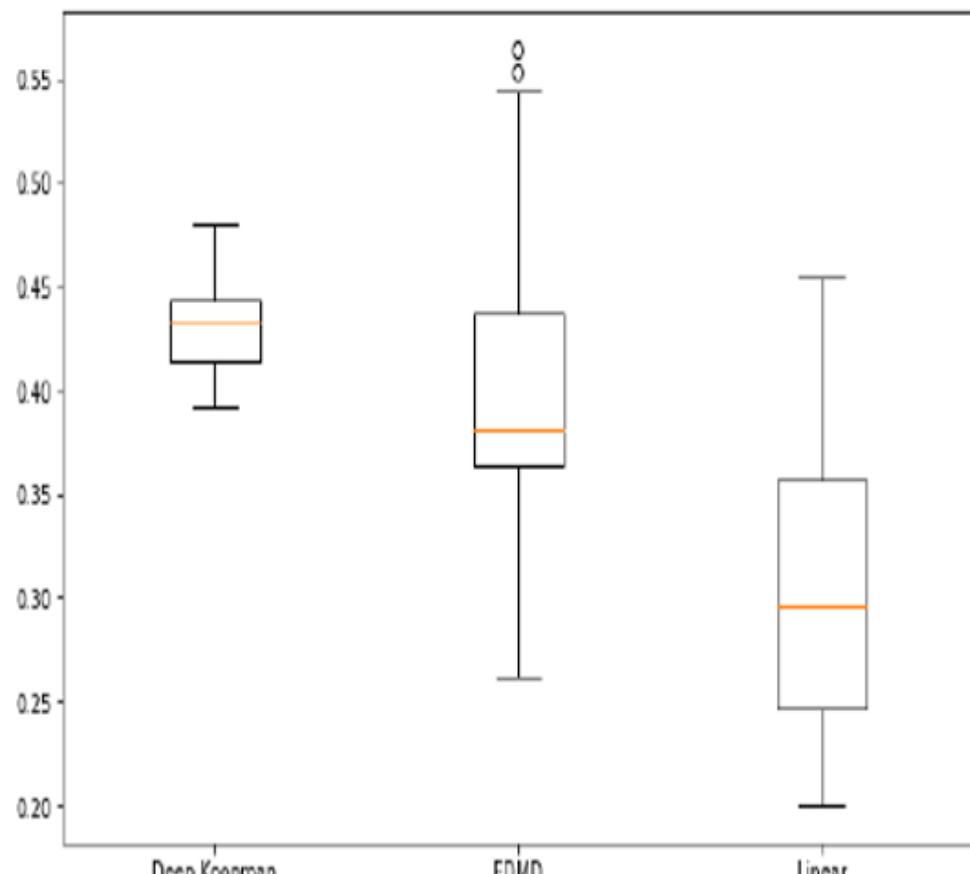


(a) Scenario 1

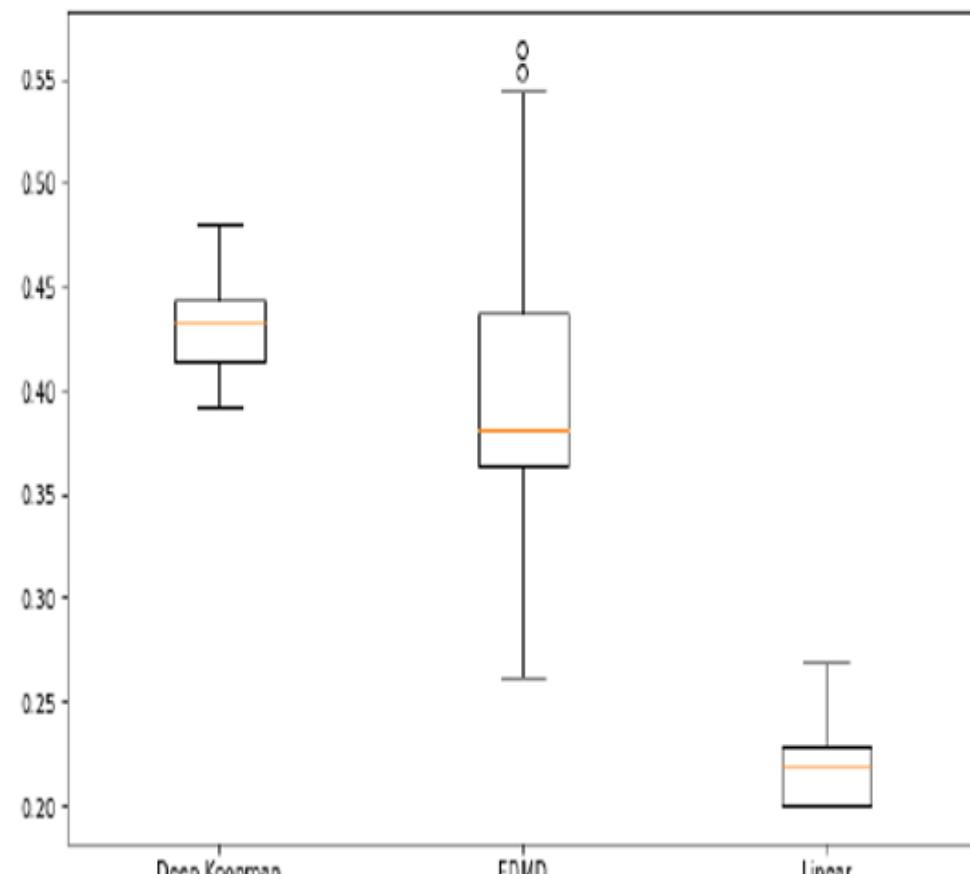


(b) Scenario 3

The Comparison of Ramp Control for On-ramp No.1



(a) Scenario 1



(b) Scenario 3

The Comparison of Ramp Control Fluctuation for On Ramp No.1

Performance Comparison of Average Objectives (ATT: Average Travel Time, ToT: Total throughput, DoC: Deviation of Control)

Approach	Scenario 1			Scenario 2			Scenario 3			Scenario 4		
	ATT	TTC	DCV									
EDMD	1571.74	32613	0.20779	1514.45	30948	0.20336	1459.89	32674	0.2293	1370.05	32723	0.15006
Linear	1626.27	32290	0.28700	1554.33	32195	0.21649	1549.06	31057	0.32817	1433.83	31608	0.32998
Fixed Control	1810.53	29403	-	1774.38	28662	-	1763.53	30582	0	1640.8	31029	0
No Control	1893.01	27998	-	1829.19	27560	-	1792.48	28903	-	1696.09	29106	-
Deep Koopman	<b>1457.96</b>	<b>34333</b>	<b>0.09384</b>	<b>1433.62</b>	<b>33951</b>	<b>0.13973</b>	<b>1363.08</b>	<b>34267</b>	<b>0.15235</b>	<b>1295.33</b>	<b>34615</b>	<b>0.11362</b>

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**THANK YOU  
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